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Invited review

On the astronomical origin of the Hallstatt oscillation found in radiocarbon and climate records throughout the Holocene

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ABSTRACT

An oscillation with a period of about 2100–2500 years, the Hallstatt cycle, is found in cosmogenic radioisotopes (^{14}C and ^{10}Be) and in paleoclimate records throughout the Holocene. This oscillation is typically associated with solar variations, but its primary physical origin remains uncertain. Herein we show strong evidences for an astronomical origin of this cycle. Namely, this oscillation is coherent to a repeating pattern in the periodic revolution of the planets around the Sun: the major stable resonance involving the four Jovian planets - Jupiter, Saturn, Uranus and Neptune - which has a period of about $p = 2318$ years. Inspired by the Milanković's theory of an astronomical origin of the glacial cycles, we test whether the Hallstatt cycle could derive from the rhythmic variation of the circularity of the solar system assuming that this dynamics could eventually modulate the solar wind and, consequently, the incoming cosmic ray flux and/or the interplanetary/cosmic dust concentration around the Earth-Moon system. The orbit of the planetary mass center (PMC) relative to the Sun was used as a proxy. We analyzed how the instantaneous eccentricity vector of this virtual orbit varies from 13,000 BCE to 17,000 CE. We found that it undergoes kind of pulsations as it clearly presents rhythmic contraction and expansion patterns with a 2318 year period together with a number of already known faster oscillations associated to the planetary orbital stable resonances, which are theoretically calculated. These periods include a quasi 20-year oscillation, a quasi 60-year oscillation, the 82-97 year Gleissberg oscillation and the 159-185 year Jose oscillation. There exists a quasi $\pi/2$ phase shift between the 2100–2500 year oscillation found in the ^{14}C record and that of the calculated eccentricity function. Namely, at the Hallstatt-cycle time scale, a larger production of radionucleotide particles occurs while the Sun-PMC orbit evolves from more elliptical shapes ($e \approx 0.598$) to more circular ones ($e \approx 0.590$), that is while the orbital system is slowly imploding or bursting inward; a smaller production of radionucleotide particles occurs while the Sun-PMC orbit evolves from more circular shapes ($e \approx 0.590$) to a more elliptical ones ($e \approx 0.598$), that is while the orbital system is slowly exploding or bursting outward. Since at this timescale the PMC eccentricity variation is relatively small ($e = 0.594 \pm 0.004$), the physical origin of the astronomical 2318 year cycle is better identified and distinguished from faster orbital oscillations by the times it takes the PMC to make pericycles and apocycles around the Sun and the times it takes to move from minimum to maximum distance from the Sun within those arcs. These particular proxies reveal a macroscopic 2318 year period oscillation, together with other three stable outer planets orbital resonances with periods of 159, 171 and 185 years. This 2318 year oscillation is found to be spectrally coherent with the $\Delta^{14}C$ Holocene record with a statistical confidence above 95%, as determined by spectral analysis and cross wavelet and wavelet coherence analysis. At the Hallstatt time scale, maxima of the radionucleotide production occurred when, within each pericycle-apocycle orbital arc, the time required by the PMC to move from the minimum to the maximum distance from the Sun varies from about 8 to 16 years while the time required by the same to move from the maximum to the minimum distance from the Sun varies from about 7 to 14 years, and vice versa. Thus, we found that a fast expansion of the Sun-PMC orbit followed by a slow contraction appears

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to prevent cosmic rays to enter within the system inner region while a slow expansion followed by a fast contraction favors it. Similarly, the same dynamics could modulate the amount of interplanetary/cosmic dust falling on Earth. Indeed, many other stable orbital resonance frequencies (e.g. at periods of 20 years, 45 years, 60 years, 85 years, 159–171–185 years) are found in radionucleotide, solar, aurora and climate records, as determined in the scientific literature. Thus, the result supports a planetary theory of solar and/or climate variation that has recently received a renewed attention. In our particular case, the rhythmic contraction and expansion of the solar system driven by a major resonance involving the movements of the four Jovian planets appear to work as a gravitational/electromagnetic pump that increases and decreases the cosmic ray and dust densities inside the inner region of the solar system, which then modulate both the radionucleotide production and climate change by means of a cloud/albedo modulation.

1. Introduction

Cosmic rays continuously collide with the Earth's atmospheric molecules fragmenting their nuclei and producing neutrons. The collisions of thermal neutrons with nitrogen nuclei ($^{14}_{7}$N made of 7 protons and 7 neutrons) give origin to cosmogenic radioisotopes ($^{14}_{6}$C made of 6 protons and 8 neutrons) according to the following reaction: $n + {}^{14}_{7}\mathrm{N} \rightarrow {}^{14}_{6}\mathrm{C} + p$. ^{14}C rapidly reacts with oxygen to produce CO_2 and, as such, is absorbed by biological organisms such as trees and marine corals. Since their formation and their capture by biological systems, ^{14}C atoms undergo a radioactive beta decay into stable ^{14}N atoms with a half-life time of 5730 years according to the following reaction: ${}^{14}_{6}\mathrm{C} \rightarrow {}^{14}_{7}\mathrm{N} + e^- + \bar{\nu}_e$. By measuring the percent of ^{14}C atoms present in a specific organic material, if the age of the latter can be timed independently, it is possible to determine the ^{14}C atmospheric concentration of the past. Determining this time series is astronomically and geophysically important because ^{14}C concentration variations are a direct consequence of changes in the intensity of the cosmic ray flux reaching the Earth, in solar magnetic activity (Bard et al., 1997; Stuiver and Quay, 1980), in the Earth's dipole moment (Elsasser et al., 1956; Lal, 1988; OBrien, 1979) and in a number of parameters regulating the radiocarbon exchange system (Goslar et al., 1999; Oeschger et al., 1975; Siegenthaler et al., 1980; Stocker and Wright, 1996).

Several experimental evidences demonstrate that ^{14}C concentration varies in time (e.g. Damon and Linick, 1986; Kromer et al., 1998, and many others). Bray (1968), using short records, and later Houtermans (1971), using records spanning throughout the Holocene (since 10,000 BCE), noted that ^{14}C concentration has changed cyclically with the longest certain period being about 2100–2500 years long. Longer oscillations could be present, but the record was too short to detect them. This period is known in the literature as the Hallstatt cycle (Vasiliev and Dergachev, 2002) because its cooling minimum occurred before the Maunder Minimum [1645:1715] happened about 2800 years ago during a late Bronze - early Iron cultural transition in an Austrian archaeological site located at Hallstatt. Other major oscillations found in the ^{14}C concentration records have periods of about 900–1050 years (Bond et al., 2001; Davis and Bohling, 2001; Kerr, 2001; Scafetta, 2012a) known in the literature as the Eddy cycle (cf. McCracken et al., 2013) and a 208-year cycle known in the literature as the Suess or de Vries cycle (Sonett, 1984). The presence of fundamental harmonics in radiocarbon records have been confirmed by numerous studies (Abreu et al., 2012; Damon, 1988; Damon and Linick, 1986; Damon et al., 1990; Damon and Sonett, 1992; Damon and Jirikowić, 1992; McCracken et al., 2013; Vasiliev and Dergachev, 1998, 2002).

An oscillation with a period of about 2100–2500 years has been found also in a number of paleoclimate records and/or events throughout the 12,000 years of the Holocene (e.g.: Dansgaard et al., 1984; Levina and Orlova, 1993; OBrien et al., 1995). For example, it was found in the δ^{18}O concentration measured in ice cores and in deep-see cores with high sedimentation rates (Pestiaux et al., 1988). Dendroclimatological considerations have also demonstrated that the Little Ice Age (1500–1800 year CE), the Hallstattzeit cold epoch (750–400 year BCE) and the earlier cold epoch (3200–2800 year BCE) are separated by 2100–2500 years (Damon and Sonett, 1992, p. 378). Given the evident correlation and synchronicity between the 2100–2500 year oscillation found in the ^{14}C concentration record and in a number of paleoclimatic data, all these records must be linked together.

Climate variations and ocean/air ventilation changes could also modulate the production of ^{14}C concentration. However, this interpretation leaves unanswered the question of why the climate would oscillate with a 2100–2500 year cycle. ^{14}C concentration could also vary because of changes in the Earth's magnetic field shielding the Earth from incoming cosmic rays (e.g. Damon and Linick, 1986). However, changes of the Earth's dipole field may be too weak to cause the 2100–2500 year oscillation in the radiocarbon records (cf.: Creer, K. M., 1988; Damon and Sonett, 1992).

Also cosmic rays, which directly form cosmogenic radioisotopes, influence the Earth's climate. Indeed, numerous empirical evidences and theoretical considerations have pointed out that cosmic rays can contribute to the formation of clouds and, therefore, modulate the Earth's albedo by ionizing the atmosphere (e.g.: Kirby, 2007; Svensmark, 1998; Svensmark et al., 2009, 2012; Tinsley, 2008), although cosmic rays alone may not explain the full amount of atmospheric precipitation variation. The existence of an astronomical origin of the involved mechanisms are also supported by the finding that variations in ^{14}C concentration are correlated with the solar system's galactic motion and imprinted in the Phanerozoic climate over the last 600 million years (e.g.: Shaviv et al., 2014).

Several authors have concluded that the observed 2100–2500 year oscillation both in the cosmogenic radioisotope records and in the climate records has a solar origin (e.g.: Dergachev and Chistyakov, 1995; Hood and Jirikowić, 1990; Hoyt and Schatten, 1997). Indeed, ^{14}C records, as well as ^{10}Be records reproduce features present in the sunspot number records such as the Maunder and Dalton solar minima, and other solar directly observed patterns (cf.: Adolphi et al., 2014; Bard et al., 1997, 2000; Scafetta, 2012a; Steinhilber et al., 2009; Usoskin et al., 2016). However, these considerations still do not explain why solar activity should vary with a 2100–2500 year oscillation. Indeed, this oscillation might also be forced on the system.

In any case, even if cosmic rays are one of the drivers of climate change, one should explain why they are modulated by a 2100–2500 years periodicity. The origin of this can be of three kinds: astronomical, solar, or Earth's endogenous. Gregori (2002) suggested that the encounters of the Solar System with clouds of interstellar matter modulate solar physics, hence its activity, and also its release of solar wind. The Earth, with its magnetosphere, captures a fraction estimated at $\sim 0.5 \times 10^{-9}$ of the surface, at 1 AU, of the expanding solar corona. That is, this is a very tiny fraction of the whole volume of the out-flowing solar wind. Similarly, the solar system is presumably capturing a very tiny fraction of the clouds of interstellar matter. These records are expected to be erratic and/or, on multi-million year time scale, they can also be modulated by the movement of

the solar system within the galaxy (cf.: Gregori, 2002; Shaviv et al., 2014). However, at the shorter time scales the incoming dust flux might be also modulated by the internal oscillating dynamics of the solar system. Hence, a very long term solar modulation could be only indicative of a galactic modulation of solar physics.

Herein we hypothesize that the 2100–2500 year oscillation in the radiocarbon records has an astronomical origin. We search whether an astronomical record clearly manifests such an oscillation. In this regard, Charvátová (2000) was the first in suggesting that the observed 2100–2500 year oscillation could be caused by the solar inertial motion, that is by the wobbling of the Sun around the barycenter of the solar system due to the orbital movements of its planets. She proposed a simplified model where the 2100–2500 year oscillation had to be on average 2402.2 years long. This period corresponds to the Jupiter/Heliocenter/barycenter alignments ($9.8855 \times 243 = 2402.2$ years). About the secular solar oscillations Charvátová (2000) showed that the inertial motion of the Sun varies from a trefoil ordered state, where the orbital patterns nearly repeat while rotating relative to the fixed stars, to a disordered one, where the orbits show confused and chaotic patterns. The ordered cases correspond to stable patterns correlated with historical solar maxima while the disordered ones correlate with historical solar minima. The latters include the Wolf minimum (1280 to 1340), the Spörer minimum (1420 to 1570), the Maunder minimum (1645 to 1715) and the Dalton minimum (1790 to 1820). Based on these patterns, the current period (1985 to 2040) could yield to a Dalton like minimum (cf.: Mörner, 2015; Scafetta, 2010, 2012a). Moreover, again using a simplified model, Scafetta (2012c) showed that the conjunctions of Jupiter and Saturn, using their tropical orbital periods, fully precess over a quasi 2400 year period.

However, the above models were oversimplified as they neglected the presence of the other planets. They could be unconvincing because the 2100–2500 year oscillation was merely implicit in calculations whose physical meaning was hypothetical. In general, it could be argued that it is physically unlikely that the solar inertial motion could be the direct cause of a variation in the solar activity because the Sun is in free-fall in it and should not feel it. A more realistic hypothesis requires that the solar inertial motion is mathematically linked to some physical mechanism yielding a variability in solar magnetic activity and/or in the incoming cosmic ray flux. The solar inertial motion could be just a proxy collecting the relevant information about the dynamics of the solar system. In principle, the planetary motion can produce gravitational and/or electromagnetic forcings directly onto the Sun, interacting with its magnetic activity, and/or within the heliosphere. In this way, it could be modulating the incoming flux of cosmic rays as well as the concentration of the interplanetary/cosmic dust around the Earth-Moon system (Ermakov et al., 2009a; Ollila, 2015). Such forcing should then maintain the imprinting of its origins and be synchronized with some planetary resonances.

Some physical mechanisms explaining a planetary modulation of solar and climate activity are currently investigated (Abreu et al., 2012; Scafetta, 2012b; Scafetta and Willson, 2013b; Wolff and Patrone, 2010). A planetary origin of solar and climate oscillations, which has been proposed since antiquity, does have numerous empirical evidences (e.g.: Abreu et al., 2012; Charvátová, 2009; Cionco and Soon, 2015; Fairbridge, 1984; Fairbridge and Sanders, 1987; Hung, 2007; Jakubcová and Pick, 1986; Jose, 1965; McCracken et al., 2013, 2014; Mörner, 2013, 2015; Mortari, 2010; Puetz et al., 2014; Salvador, 2013; Scafetta, 2010, 2012a,b, 2013, 2014, 2016; Scafetta and Willson, 2013a,b; Sharp, 2013; Solheim, 2013; Tan and Cheng, 2013; Tattersall, 2013a,b; Wilson, 2013).

The present work aims to provide a robust evidence that the 2100–2500 year Hallstatt oscillation found both in cosmogenic radioisotopes and in climate records throughout the Holocene has an astronomical origin linked to a major recurrence of particular displacements of the planets around the Sun. In the choice of the appropriate astronomical proxy, we were inspired by the Milanković (1930) theory that links the ~100,000 year variation of the Earth's orbit eccentricity to the glacial cycles of the past 1 million years. Thus, we hypothesize that the Hallstatt cycle could derive from an expansion-contraction rhythmic dynamics of the solar system driven by the rotation of the planets that yields to a specific set of stable orbital resonances that will be also theoretically calculated.

The dynamics of the solar system circularity is well described by the wobbling of the planetary mass center (PMC) orbiting the Sun, which scales the wobbling of the Sun relative to the barycenter of the solar system. We used the ephemeris of the Sun relative to the barycenter to derive such a complex orbit. Then we used a proposed Keplerian constant of motion, the eccentricity vector (e.g.: Mungan, 2005), to evaluate how the instantaneous eccentricity of the orbit of the PMC varies in time. Using this observable we demonstrate that the solar system circularity pulses with a 2100–2500 period together with a number of already known oscillations associated to the orbital periods of the planets.

The situation of having several stable orbital resonances and orbital proxies made of many harmonics is not surprising because of the complexity of the solar system. It is, however, highly confusing for identifying the possible physical origin of a specific oscillation. The evident analogous is the theory of ocean tides where generic tidal generation potentials deduced from the Sun's and Moon's orbits relative to the Earth produce a very large number of tidal constituent waves (Doodson, 1921; Melchior, 1978). These oscillations are differentiated in the literature with a very long list of Darwin's symbols indicating their physical origin such as the *N* (lunar Saros) tidal wave, *Sa* (solar annual) tidal wave, *Mm* (lunar monthly) tidal wave, *M*2 (principal lunar semidiurnal) tidal wave, the *S*2 (principal solar semidiurnal) tidal wave, and *N*2 (larger lunar elliptical semidiurnal) tidal wave (Darwin, 1902). Alternative and specific astronomical proxies are needed to well highlight each of these oscillations because they have a different physical origin and many of them are just small perturbations of the dominant *M*2 and *S*2 waves.

To better identify the physical origin of the astronomical 2100–2500 year cycle, and to separate it from the fast and larger oscillations associated to the orbits of the planets, we searched for more appropriate astronomical proxies. We collected the times it takes the Sun to make pericycles and apocycles and the times it takes the Sun to move from its minimum to maximum distances from the barycenter within these arcs. We show that these particular astronomical proxies reveal a macroscopic 2100–2500 year period oscillation perfectly coherent to the Hallstatt oscillation found in the radionucleotide records with a statistical confidence above 95%.

Finally, we briefly hypothesize the physical mechanisms involved in the process suggesting that the pulses of the solar system could be modulating the solar wind and by that the incoming cosmic ray flux and the cosmic dust concentration surrounding the Earth (cf.: Mörner, 1996).

2. The 2100–2500 year Hallstatt cycle in the $\Delta^{14}C$ nucleotide record

Fig. 1A shows the $\Delta^{14}C$ (‰) record (IntCal04.14c) from 10,500 BCE to 1845 CE that covers the entire Holocene (data are from Reimer et al., 2004). This record was obtained using dendrochronological dating and cross-checking from several millennia-long tree-ring chronologies. The IntCal04.14c record extends for 26,000 years. The last 12,500 years are reported with a 5-year resolution and the data derive mostly from tree-ring chronologies. For older dates this record is made using mostly marine (e.g. coral) records that have a lower resolution. The second component of the record, the one

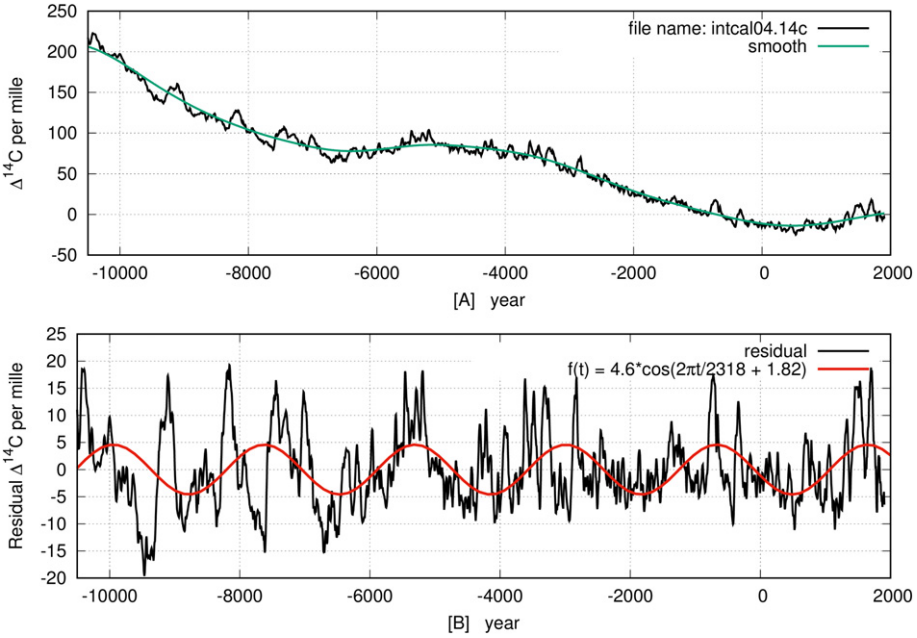

Fig. 1. [A] $\Delta^{14}C$ (‰) record (black) throughout the Holocene from −10,500 BCE to 1900 CE and its multi-millennial smooth curve (green). [B] A residual signal obtained by detrending the smooth curve from the data. The latter is a fit with a sinusoidal function (red). This signal covers the period from 10,500 BCE to 1900 CE. The figures report the name of the original file downloaded from https://www.radiocarbon.org/IntCal04.htm. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

obtained mostly from marine chronologies, is not used here because it shows altered and very smooth patterns compared to the tree-ring chronologies. This difference is very likely due to the diverse physical properties of the two sets as one uses trees that absorb carbon directly from the air where ^{14}C is produced by cosmic rays, while the other uses corals that absorb carbon dissolved in the water where it can remain diluted for very long times.

Fig. 1A also shows in green a gnuplot acsplines smooth curve that captures the multi-millennial modulation of the record that appears to be characterized by a trend plus an approximate 6000–7000 year modulation, which is observed throughout the entire 26,000 years of the original record. The physical origin of the trend and this long oscillation are not discussed herein. Fig. 1B shows the residual signal obtained by detrending the smooth curve from the original data from 10,500 BCE to 1900 CE. Note that since 1900 the radionucleotide record has been likely contaminated from increasing anthropogenic CO_2 emissions and since 1950 because of atmospheric nuclear bomb tests.

The residual record depicted in Fig. 1B is relatively similar to the data made available in file Resid04_2000.14c (Reimer et al., 2004) where a smoothing spline approximating a 2000-year moving average was used (cf.: Stuiver et al., 1998). However, our adopted filtering is significantly smoother and better preserves the patterns at scales shorter than 5000 years. This operation avoids artifacts that might interfere with the Hallstatt cycle.

The residual record presents two major oscillations at about 900–1050 year period (the Eddy cycle) and at 2100–2500 year period (the Hallstatt cycle): see the periodogram in Fig. 10 commented in Section 7. The quasi millennial oscillation found in nucleotide record has been extensively studied in the literature. It was found coherent with a quasi-millennial climate large oscillation (e.g.: Bond et al., 2001; Kerr, 2001) and was reconstructed with a combination of Jupiter-Saturn tidal induced oscillations and the 11-year sun-spot oscillation (e.g.: Scafetta, 2012b, 2014). Herein, we will not focus on this oscillation either, but only on the longer Hallstatt cycle.

We attempted to fit the residual record depicted in Fig. 1B with a harmonic curve of the type

$$f(t) = A\cos(2\pi t/T + \phi) + C. \quad (1)$$

However, the statistical fit gives slightly different values according to the chosen time interval. For example: from 6000 BCE to 1900 CE it gives $T = 2357 \pm 24$ years; from 7000 BCE to 1900 CE it gives $T = 2326 \pm 18$ years; from 8000 BCE to 1900 CE it gives $T = 2249 \pm 16$ years; from 9000 BCE to 1900 CE it gives $T = 2311 \pm 15$ years; and from 10,500 BCE to 1900 CE it gives $T = 2402 \pm 14$ years. The harmonic function fit also gives a slightly variable phase according to the fit interval of about $\phi = 2 \pm 0.2$.

Such a variable result is not surprising in analyzing experimental geophysical, radionucleotide or paleoclimatic records spanning several thousands years since these records are characterized by some uncertainty both in the amplitude and in the timing of the data. Moreover, the records may be influenced by different physical sources that could induce a certain pattern variability. In any case, since the statistical error of the periodogram associated to a spectral peak period is $\nabla p = \pm p^2/2L$, where $L = 12,500$ years is the length of the record shown in Fig. 1B, an observed spectral peak period at the 2100–2500 year time scale is characterized by a spectral error of about ±200 years, which well covers the typical uncertainty range found in radionucleotide (^{14}C and ^{10}Be) records regarding the Hallstatt cycle, as reported in the scientific literature.

Given the above uncertainty, in Fig. 1B we fit the record with an harmonic function with period $T = 2318$ years for the reasons explained in Section 3 and also because such period is nearly recovered by the fit value from 9000 BCE to 1900 CE. that covers the Holocene after the end of the last glacial period.

The harmonic function depicted in Fig. 1B uses the fit parameters obtained during the period between 750 BCE and 1750 CE, which covers the first Hallstatt oscillation observed in the radionucleotide

record. During this period the data are likely the most accurate of the record because the uncertainty increases with time. The phase shift of the harmonic function is $\phi = 1.82$. Thus, the maximum of the radiocarbon Hallstatt cycle corresponds to about 1645 CE, namely the beginning of the Maunder solar Minimum [1645–1715], which was the most significant solar minimum of the last millennium.

As shown in Fig. 1B, the depicted harmonic function well predicts the previous Hallstatt maxima in the radionucleotide record that corresponded to the coldest epochs of the Holocene occurred around these periods: 10,000 BCE(Younger Dryas cooling onset), 7500 BCE(Early Holocene cooling event), 5300 BCE(Boreal/Atlantic transition and precipitation change), 3000 BCE(Mid-Holocene Transition.), 700 BCE(Sub-Atlantic Minimum that also yielded the Greek Dark Ages). Indeed, OBrien et al. (1995) found that also the polar atmospheric circulation changes are regulated by a Hallstatt oscillation throughout the Holocene. A cooling-warming cycle of about 2100–2500 years is, indeed, observed throughout the Holocene in numerous climate records (e.g.: Bond et al., 2001; Marcott et al., 2013; Mayewski et al., 2004). Also a quasi millennial cycle is observed in climate and radionucleotide records (cf.: Bond et al., 2001; Kerr, 2001; Scafetta, 2013, 2014).

In any case, note that the adoption of a fit phase of about $\phi = 2$ would induce a temporal shift of about 65 years relative to the chosen harmonic depicted in Fig. 1B, and the maximum of the 2318 year cycle would fall in 1580 CE, which is between the Spörer solar Minimum [1450–1550] and the Maunder Minimum [1645–1715]. Thus, in any case, the strong solar minimum of the 16th–17th centuries was likely driven by the Hallstatt cycle. For the purpose of this paper the difference between the two phases is nearly negligible.

3. The Jupiter-Saturn-Uranus-Neptune 2318-year stable resonance

An important concept in celestial mechanics is that of orbital resonance. A resonance occurs when two or more orbiting bodies can exert a regular, periodic gravitational influence on each other. This happens when their orbital periods are related by a ratio of small integers. Orbital resonances greatly enhance the mutual gravitational influence of the bodies and, therefore, of the space symmetry of an orbiting system such as the heliosphere of the solar system. Well known examples of orbital resonances are the 1:2:4 resonance of Jupiter's moons Ganymede, Europa and Io, the 2:3 resonance between Pluto and Neptune, the various resonances that regulate the asteroid belt etc. Indeed, the entire solar system appears to be synchronized by specific orbital resonances (cf. Scafetta, 2014b; Tattersall, 2013a). Thus, we hypothesize that the Hallstatt oscillation found in radionucleotide and climatic records could be the result of a specific orbital resonance within the solar system. All planets could be involved in the process but, because of the length of the Hallstatt oscillation, it is more reasonable to search a resonance that links the four Jovian planets: Jupiter, Saturn, Uranus and Neptune.

A system of periods T_i is said to be in linear resonant state if there exists a set of small integer numbers a_i such that:

$$\frac{1}{T} = \left| \sum \frac{a_i}{T_i} \right| < \gamma, \tag{2}$$

where $i = 1, \ldots, N$. N is the number of orbiting objects, γ a very small number and T the resonance period. The simplest case of resonance is when two orbital periods (e.g. P_1 and P_2) have an integer ratio: $P_1/P_2 = n$, where n is the integer 1, 2 or 3 etc.

A linear resonance is also stable if its resonance order is zero, that is if $\sum a_i = 0$. Stable resonances are independent on the selection of the rotating reference system. In fact, relative to any observer moving with any period M with regard to stars, each orbital body would rotate with a frequency $f_{iM} = 1/T_i - 1/M$. It is easy to demonstrate that for stable resonances it holds: $T^{-1} = \sum a_i/T_i = \sum a_i f_{iM}$. Therefore, stable resonances significantly characterize the physical properties of an orbital system because may favor the emergence of additive and synchronized forcing on a rotating system such as the Sun or the heliosphere.

The simplest cases of stable resonances are the synodical periods between two orbiting objects whose frequency is given by $f_{12} = |1/P_1 - 1/P_2|$. For example: the synodic or conjunction period between Jupiter ($P_J = 4332.589$ days) and Saturn ($P_S = 10759.22$ days) is $P_{JS} = (P_J^{-1} - P_S^{-1})^{-1} = 7253.455$ days $= 19.859$ years; the synodic or conjunction period between Uranus ($P_U = 30685.4$ days) and Neptune ($P_N = 60189.0$ days) is $P_{UN} = \left(P_U^{-1} - P_N^{-1}\right)^{-1} = 62599.94$ days $= 171.393$ years. The orbital periods are from NASA (http://nssdc.gsfc.nasa.gov/planetary/factsheet/); we use the conversion: 1 year $= 365.2425$ days.

There are very few stable orbital resonances and if the coefficients a_i, which must be small, are chosen between −3 and 3 only one resonance falls within the Hallstatt time scale of 2100–2500 years and, in general, for periods larger than 200 years. This is a combination of the orbital periods of Jupiter, Saturn, Uranus and Neptune such that:

$$f_{JSUN} = \frac{1}{P_j} - \frac{3}{P_S} + \frac{1}{P_U} + \frac{1}{P_N}. \tag{3}$$

The period of such a resonance is

$$P_{JSUN} = \frac{1}{f_{JSUN}} = 846471.447\ d = 2317.56\ year. \tag{4}$$

Since the above resonance is stable, the same period can be determined by any observer moving with any period M with regard to stars. The physical meaning of the above resonance will be demonstrated in the following sections. Herein we stress that this resonance involves a combination of all four Jovian planets. We also notice that such a resonance nearly corresponds to about 116.5 revolutions of the conjunction period of Jupiter and Saturn ($116.5 * 19.859 = 2313.6$ years), and 13.5 revolutions of the conjunction period of Uranus and Neptune ($13.5 * 171.393 = 2313.8$ years). Thus, every about 2313.7 years there exists a repeating pattern involving conjunctions and oppositions among the four Jovian planets of the solar system whose gravitational effect is revealed in the following sections.

Additional resonances can be calculated by making the coefficients a_i to vary within a larger range. However, even if this range is chosen to be between −10 and 10, the only stable resonance periods found for periods larger than 1000 years are at 1158.78 years (resonance 2:−6:2:2), 1159.30 years(resonance −1:2:4:−5), 2317.56 years (resonance 1:−3:1:1), 2319.62 years (resonance −2:5:3:−6) and 2,607,251.87 years (resonance 3:−8:−2:7). Thus, the period of 2317–2320 years represents a very important and unique stable resonance of the solar system. We note that Humlum et al. (2011) found a 1139 ± 160 year oscillation in the detrended GISP2 surface temperature series during the last 4000 years and Davis and Bohling (2001) found a spectral peak between 950 years and 1113 years, which may be coherent to the above millennial stable resonances although for the Eddy cycle there could be alternative explanations (e.g.: Scafetta, 2012a, 2014).

Two other important stable resonances that we will meet in the next sections are:

$$f_{JSU} = \frac{1}{P_J} - \frac{3}{P_S} + \frac{2}{P_U}, \tag{5}$$

which gives $P_{JSU} = 159.59$ years and

$$f_{JSN} = -\frac{1}{P_J} + \frac{3}{P_S} - \frac{2}{P_N}, \quad (6)$$

which gives $P_{JSN} = 185.08$ years.

We will demonstrate that, using opportune astronomical observables, the 2318-year resonance appears like a modulation of these faster resonance oscillations together with that of the Uranus-Neptune synodic stable resonance $P_{UN} = 171.393$ years. The three 159–171–185 year astronomical resonances are very important also for supporting the main hypothesis of our paper, namely to interpret astronomically the origin of the Hallstatt oscillation observed in radionucleotide and climate records. In fact, these resonances, in particular P_{UN}, have already been found to characterize such geophysical records used to reconstruct also cosmic ray flux and solar activity throughout the Holocene (cf.: McCracken et al., 2014; Sharp, 2013) and also with aurora records available since the 16th century (Scafetta and Willson, 2013a).

Table 1 reports a list of stable resonances for periods larger than 5 years associated to the Jupiter-Saturn-Uranus-Neptune system where the coefficients a_i are made to vary between −3 and 3. These resonances are clustered around specific frequencies. In particular, note the resonance clusters at 44–46 years, 57–62 years and 82–97 years that are found in solar and aurora activity (e.g.: McCracken et al., 2001; Ogurtsov et al., 2002; Scafetta, 2014; Scafetta and Willson, 2013a; Vaquero et al., 2002) and also in climate records (e.g.: Czymzik et al., 2016; Hoyt and Schatten, 1997, and many others). For example, a quasi 60-year cycle is very important in climate (e.g.: Gervais, 2016; Loehle and Scafetta, 2011; Manzi et al., 2012; Mazzarella and Scafetta, 2012; Scafetta, 2010, 2014c; Wyatt and Curry, 2014, and many others). The 82–97 year period is known as the Gleissberg cycle.

In the next section we will construct physical observables that better reveal the above Jupiter-Saturn-Uranus-Neptune resonances. From a purely spectral point of view, it may be pointed out that many functions of the orbits of the planets (e.g. total angular momentum of the planets, speed and position of the PMC relative to the Sun) are expected to present numerous common spectral peaks simply because their harmonic input is the same. We will use the eccentricity function of the Sun-PMC orbit and other specific orbital proxies because these proxies suggest a possible physical mechanism, as we will discuss in the next sections.

Table 1
Stable resonances associated to the Jupiter-Saturn-Uranus-Neptune system. The coefficients a_i of Eq. (2) are made to vary between −3 and 3. See also Fig. 4B.

a_{Jup}	a_{Sat}	a_{Ura}	a_{Nep}	T (year)	a_{Jup}	a_{Sat}	a_{Ura}	a_{Nep}	T (year)
3	−1	−2	0	5.12	2	−2	−2	2	11.23
2	2	−3	−1	5.14	1	1	−3	1	11.29
3	−2	2	−3	5.25	2	−3	2	−1	11.83
3	−1	−3	1	5.28	1	0	1	−2	11.90
3	−2	1	−2	5.41	0	3	0	−3	11.96
2	1	0	−3	5.42	2	−2	−3	3	12.02
3	−2	0	−1	5.59	2	−3	1	0	12.71
2	1	−1	−2	5.60	1	0	0	−1	12.78
3	−2	−1	0	5.78	0	3	−1	−2	12.85
2	1	−2	−1	5.79	2	−3	0	1	13.73
3	−3	3	−3	5.93	1	0	−1	0	13.81
3	−2	−2	1	5.98	0	3	−2	−1	13.90
2	1	−3	0	5.99	1	−1	3	−3	14.74
3	−3	2	−2	6.15	2	−3	−1	2	14.93
2	0	1	−3	6.16	1	0	−2	1	15.02
3	−2	−3	2	6.19	0	3	−3	0	15.12
3	−3	1	−1	6.37	1	−1	2	−2	16.12
2	0	0	−2	6.39	0	2	1	−3	16.24
1	3	−1	−3	6.41	2	−3	−2	3	16.35
3	−3	0	0	6.62	1	0	−3	2	16.47
2	0	−1	−1	6.64	1	−1	1	−1	17.80
1	3	−2	−2	6.66	0	2	0	−2	17.93
3	−3	−1	1	6.89	1	−1	0	0	19.86
2	0	−2	0	6.91	0	2	−1	−1	20.03
1	3	−3	−1	6.93	1	−1	−1	1	22.46
2	−1	2	−3	7.13	0	2	−2	0	22.68
3	−3	−2	2	7.17	1	−2	3	−2	25.01
2	0	−3	1	7.20	0	1	2	−3	25.29
2	−1	1	−2	7.44	1	−1	−2	2	25.85
1	2	0	−3	7.46	0	2	−3	1	26.14
3	−3	−3	3	7.49	1	−2	2	−1	29.29
2	−1	0	−1	7.78	0	1	1	−2	29.66
1	2	−1	−2	7.80	1	−1	−3	3	30.44
2	−1	−1	0	8.15	1	−2	1	0	35.32
1	2	−2	−1	8.18	0	1	0	−1	35.87
2	−2	3	−3	8.46	1	−2	0	1	44.49
2	−1	−2	1	8.55	0	1	−1	0	45.36
1	2	−3	0	8.58	0	0	3	−3	57.13
2	−2	2	−2	8.90	1	−2	−1	2	60.09
1	1	1	−3	8.93	0	1	−2	1	61.69
2	−1	−3	2	9.00	1	−3	3	−1	82.64
2	−2	1	−1	9.39	0	0	2	−2	85.70
1	1	0	−2	9.42	−1	3	1	−3	88.99
2	−2	0	0	9.93	1	−2	−2	3	92.54
1	1	−1	−1	9.97	0	1	−3	2	96.39
2	−2	−1	1	10.54	1	−3	2	0	159.59
1	1	−2	0	10.59	0	0	1	−1	171.39
2	−3	3	−2	11.07	−1	3	0	−2	185.08
1	0	2	−3	11.12	1	−3	1	1	2317.56

4. The eccentricity vector

Let us fully derive the instantaneous eccentricity function of the orbit of a generic planet orbiting the Sun (cf.: Mungan, 2005). In classical celestial mechanics a Keplerian orbit is defined as the motion of an object orbiting another (e.g. a planet orbiting its star) under Newton's force of gravity:

$$m\boldsymbol{a} = -\frac{GMm}{r^2}\hat{\boldsymbol{r}}, \quad (7)$$

because $\boldsymbol{r} = r\hat{\boldsymbol{r}}$ and the angular momentum $\boldsymbol{L} = m\boldsymbol{r} \times \boldsymbol{v}$ is constant, Eq. (7) can be easily rewritten as

$$\frac{d}{dt}(\boldsymbol{v} \times \boldsymbol{L}) = GMm\frac{d\hat{\boldsymbol{r}}}{dt}, \quad (8)$$

where $\boldsymbol{v} = d\boldsymbol{r}/dt$ is the velocity of the orbiting body. By integrating Eq. (8), we obtain

$$\boldsymbol{v} \times \boldsymbol{L} = GMm(\hat{\boldsymbol{r}} + \boldsymbol{e}), \quad (9)$$

where $\boldsymbol{e}$ is an integration constant vector. After some vector algebra we obtain

$$\boldsymbol{e} = \frac{\boldsymbol{v} \times (\boldsymbol{r} \times \boldsymbol{v})}{GM} - \hat{\boldsymbol{r}}. \quad (10)$$

To understand the physical meaning of the vector $\boldsymbol{e}$, we take the dot product of the position vector $\boldsymbol{r}$ with Eq. (9) to obtain

$$\boldsymbol{r} \cdot (\boldsymbol{v} \times \boldsymbol{L}) = GMm\boldsymbol{r} \cdot (\hat{\boldsymbol{r}} + \boldsymbol{e}) \quad (11)$$

that becomes

$$m(\boldsymbol{r} \times \boldsymbol{v}) \cdot \boldsymbol{L} = L^2 = GMm^2(1 + e\cos\theta)r. \quad (12)$$

If $c = L^2/(GMm^2)$ and the vector $\boldsymbol{e}$ is chosen to point toward the periapsis of the orbit, in the traditional $r-\theta$ polar coordinates, Eq. (12) is equivalent to the traditional Keplerian orbital equation:

$$r(\theta) = \frac{c}{1 + e\cos\theta}, \tag{13}$$

where c is a constant called the semi-latus rectum of the curve and e is the eccentricity of the orbit.

For a circular orbit $e = 0$; for an elliptical orbit $0 < e < 1$ and $\theta = 0$ and $\theta = \pi$ indicate the position of the perihelion and aphelion, respectively; for a parabolic trajectory $e = 1$; and for a hyperbolic trajectory $e > 1$. In the case of a simple two-body system, without any form of dissipation or perturbation, celestial mechanics predicts that the eccentricity e of an orbit is constant. Thus, Eq. (10) defines the eccentricity vector, whose scalar is the eccentricity of the Keplerian orbit.

Using simple vector algebra, $\boldsymbol{v}\times(\boldsymbol{r}\times\boldsymbol{v}) = (\boldsymbol{v}\cdot\boldsymbol{v})\boldsymbol{r} - (\boldsymbol{r}\cdot\boldsymbol{v})\boldsymbol{v}$, Eq. (10) can be rewritten in a more friendly way, and the instantaneous eccentricity of the trajectory of each planet of the solar system can be defined as

$$e = \left|\left(\frac{v^2}{\mu} - \frac{1}{r}\right)\boldsymbol{r} - \frac{\boldsymbol{r}\cdot\boldsymbol{v}}{\mu}\boldsymbol{v}\right|, \tag{14}$$

where $\mu = GM_{sun} = 2.959122082855911\cdot10^{-4}$ AU^3/d^2 is the standard gravitational parameter for the Sun as used in the adopted ephemeris files (Folkner et al., 2014, Table 8). However, Eq. (7) works if $M \gg m$. In real cases, the mass m on the left side of Eq. (7) must be substituted with the reduced mass, $M_{sun}m_{planet}/(M_{sun} + m_{planet})$, which yields again to Eq. (14) with the following correction $\mu = G(M_{sun} + m_{planet})$, as we will use in the following section.

5. Definition of the planetary mass center relative to the Sun

The wobbling of the Sun occurs mostly close to the ecliptic orbital plane and it is a real feature of the solar system relative to the outer deep space from where the cosmic ray flux comes. We hypothesized that the rhythmic contraction and expansion of the solar system associated to its inner wobbling could modulate the incoming cosmic ray flux reaching the Earth and/or alter the physical properties of the heliosphere modulating the solar wind and interplanetary/cosmic dust concentration. This dynamics can be represented by the movement of the planetary mass center (PMC) relative to the Sun. This orbit is deduced by using programs that implement the ephemeris files DE431/DE432 prepared by the NASA Solar System Dynamics Group of the Jet Propulsion Laboratory (ftp://ssd.jpl.nasa.gov/pub/eph/planets/ascii) (Folkner et al., 2014; Folkner, 2014).

Folkner et al. (2014) reports that the orientation of the DE431/DE432 ephemeris is tied to the International Celestial Reference Frame with an accuracy of 0.0002″: for the inner planets the orbital accuracy is of the order of a few hundred meters, for Jupiter and Saturn the orbital accuracy is of tens of kilometers and for Uranus, Neptune, and Pluto the orbital accuracy worsen up to several thousand kilometers. This means that the orbital parameters have at least a 9 to 7 digit precision from the inner planets up to Pluto, respectively. Thus, the ephemeris error-bars alone are not expected to provide false evidences for major cycles, also because several of the observed spectral peaks of the adopted astronomical observables can be easily recognized as stable orbital resonances or orbital periods, as shown below.

Let $\boldsymbol{r}_p$ be the vector position of the center of mass of all objects of the solar system, Sun excluded, relative to the barycenter; let $\boldsymbol{r}_s$ be the vector position of the Sun relative to barycenter; let M_p be the total mass of all objects of the solar system excluded the Sun, that is the sum of the 352 masses (planets + asteroids) taken into account by the DE432 JPL ephemeris file; let M_s be the mass of the Sun. These masses are deduced from the parameters of the header file of the NASA JPL DE432 ephemeris file.

Relative to the barycenter, the position vectors and the relative velocities are balanced, that is, observing that $M_p\boldsymbol{r}_p = \sum_i m_i\boldsymbol{r}_i$ and $M_p\boldsymbol{v}_p = \sum_i m_i\boldsymbol{v}_i$ where the index i refers to each planetary or asteroid object of the solar system, the following equations are fulfilled:

$$M_s\boldsymbol{r}_s + M_p\boldsymbol{r}_p = 0 \tag{15}$$

$$M_s\boldsymbol{v}_s + M_p\boldsymbol{v}_p = 0. \tag{16}$$

Let $\boldsymbol{r}$ and $\boldsymbol{v}$ be the position and velocity vector, respectively, of the PMC relative to the Sun. Thus, we have:

$$\boldsymbol{r} = -\boldsymbol{r}_s + \boldsymbol{r}_p = \frac{M_s + M_p}{M_p}(-\boldsymbol{r}_s) \tag{17}$$

$$\boldsymbol{v} = -\boldsymbol{v}_s + \boldsymbol{v}_p = \frac{M_s + M_p}{M_p}(-\boldsymbol{v}_s) \tag{18}$$

Fig. 2 shows a section of the orbit of PMC from 1950 to 2050 where it is seen that the PMC point wobbles around the Sun within an orbit of about 7 AU radius.

Although Eq. (14) can be rigorously applied only to a Keplerian orbit, and is useful to determine for example the small fluctuations of the orbits of the planets of the solar system, we can assume that the PMC, which does not follow a Keplerian orbit, at each instant represents a given planet P that is orbiting the Sun at that specific position $\boldsymbol{r}$ and with that specific velocity $\boldsymbol{v}$ estimated in Eqs. (17) and (18). Then, we define the instantaneous eccentricity of the orbit of PMC as the eccentricity of the hypothetical orbit of the planet P evolving in time using Eq. (14), the $\boldsymbol{r}$ and $\boldsymbol{v}$ vectors estimated in Eqs. (17) and (18) and $\mu = G(M_s + M_{CMP}) = 2.963092749817812\cdot10^{-4}$ AU^3/d^2, which takes into account all masses of the solar system used in the ephemeris files DE431/DE432.

6. Analysis of the "eccentricity" variation of the Sun-PMC orbit

Fig. 3 shows the record of the eccentricity e of the Sun-PMC orbit calculated by Eq. (14) from 13,000 BCE to 17,000 CE. sampled every 30 days. Fig. 4A shows its periodogram and Fig. 4B compares it with the periods of the stable planetary resonances reported in Table 1. A clear correspondence is found between all spectral peaks of the eccentricity function of the Sun-PMC orbit and the stable resonances generated by Jupiter, Saturn, Uranus and Neptune.

As expected, the instantaneous eccentricity of the Sun-PMC orbit varies greatly from a trajectory nearly circular ($e \approx 0$) to one nearly parabolic ($e \approx 1$). Large oscillations are observed, in particular at the 19.86 year synodic period between Jupiter and Saturn. Other strong oscillations close to the known planetary orbital periods of the four Jovian planets are observed: Jupiter, 11.86 years; Saturn, 29.46 years; Uranus, 84.01 years; Neptune, 164.8 years. In addition, several other synodic periods among planets are observed as well: Earth-Jupiter, 1.092 years; Jupiter-Uranus, 13.8 years; Jupiter-Neptune, 12.78 years; Saturn-Uranus, 45.4 years; Saturn-Neptune, 38.9 years; Uranus-Neptune, 172 years. Also the Jupiter-Saturn trigon synodic period, 57–61 years, is well observed. All these known oscillations were well expected although their accurate values appear to be given by the stable orbital resonances listed in Table 1.

For what concerns this study, Figs. 3 and 4 also demonstrate that the chosen eccentricity function presents a major oscillation at about 2100–2500 year period that could not be immediately derived from the individual planetary orbital periods. The statistical error of the

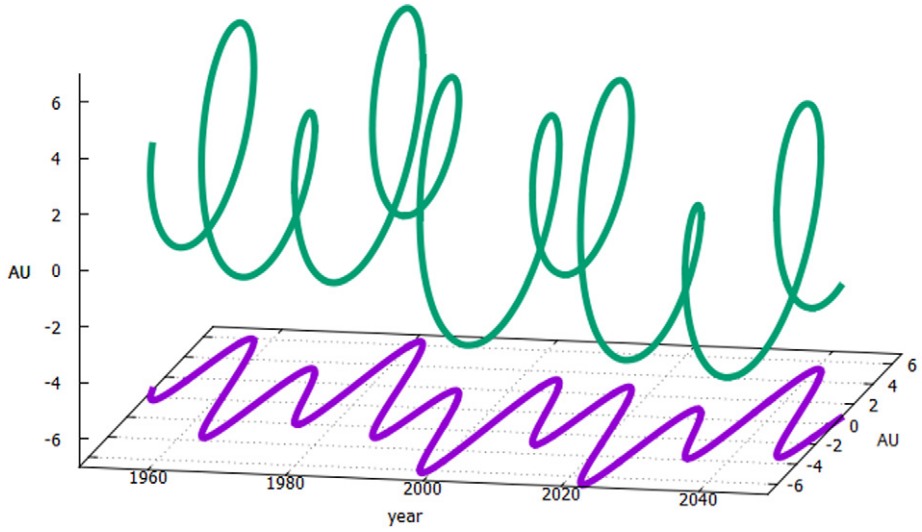

Fig. 2. Motion of the PMC relative to the Sun from 1950 to 2050.

periodogram associated to a spectral peak period is $\nabla p = \pm p^2/2L$, where $L = 30,000$ years is the length of the record analyzed. The observed periodogram peak period is at $p = 2318 \pm 90$ years. Thus, it is evidently due to the Jupiter-Saturn-Uranus-Neptune resonance discussed in Section 3. This periodicity is perfectly coherent with the Hallstatt oscillation found in the radionucleotide records as that shown in Figs. 1: see Fig. 10. The periodogram depicted in Fig. 4 stresses that the 2318 year period peak is the most relevant within the spectral range between 200 and 10,000 year periods indicating that this oscillation dominates this time scale, as also found for the stable resonances reported in Table 1 .

Fig. 5 compares the cosine curves used to fit both the radionucleotide record depicted in Fig. 1B, and the eccentricity function depicted in Fig. 3. The periods are the same, within their error of measure, and the phases are $\phi \approx 1.82$ and $\phi \approx 3.24$, respectively. Thus, as Fig. 5 (upper panel) shows, the two harmonics are shifted by almost $\pi/2$ or about 525 years. This means that the Hallstatt oscillation of the radionucleotide record is nearly proportional to the integration or to the negative of the derivative of the eccentricity record of the Sun-PMC orbit.

Fig. 5 shows that, on the Hallstatt-cycle time scale, a larger production of radionucleotide particles occurs while the Sun-PMC orbit evolves from statistically more elliptical shapes ($e \approx 0.598$) to statistically more circular ones ($e \approx 0.590$), that is while the system is bursting outward. Analogously, a smaller production of radionucleotide particles occurs while the Sun-PMC orbit evolves from statistically more circular shapes ($e \approx 0.590$) to statistically more elliptical ones ($e \approx 0.598$), that is while the system is bursting inward.

Fig. 5 (lower panels) shows trajectories of the Sun-PMC orbits when these are statistically more elliptical (upper list of lower panels, the average eccentricity is $e \approx 0.598$) and when these are

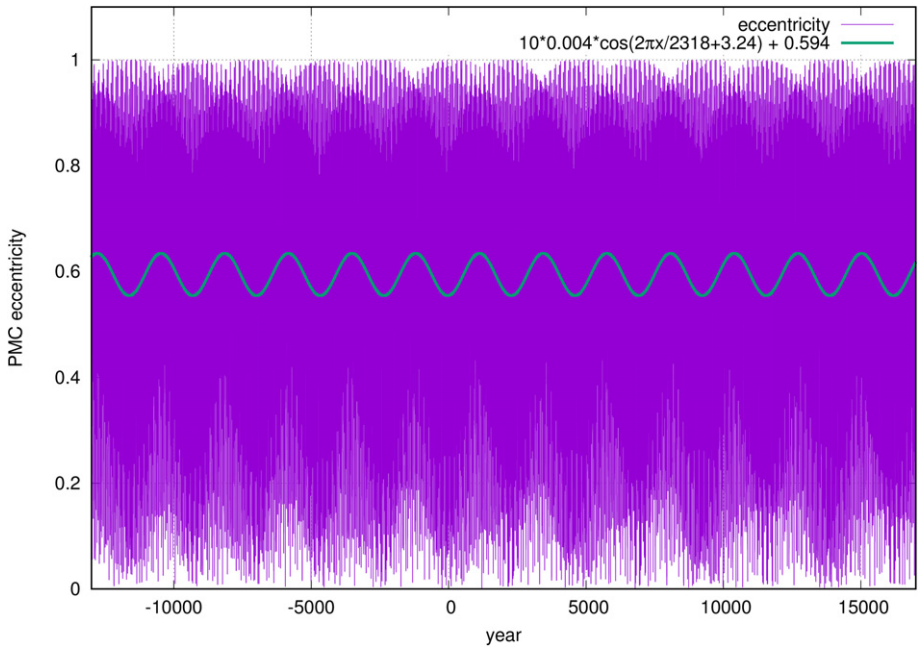

Fig. 3. Variation of the eccentricity (Eq. (14)) of the PMC relative to the Sun. The latter is fit with a sinusoidal function (green) whose amplitude has been magnified by 10 for visual convenience. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

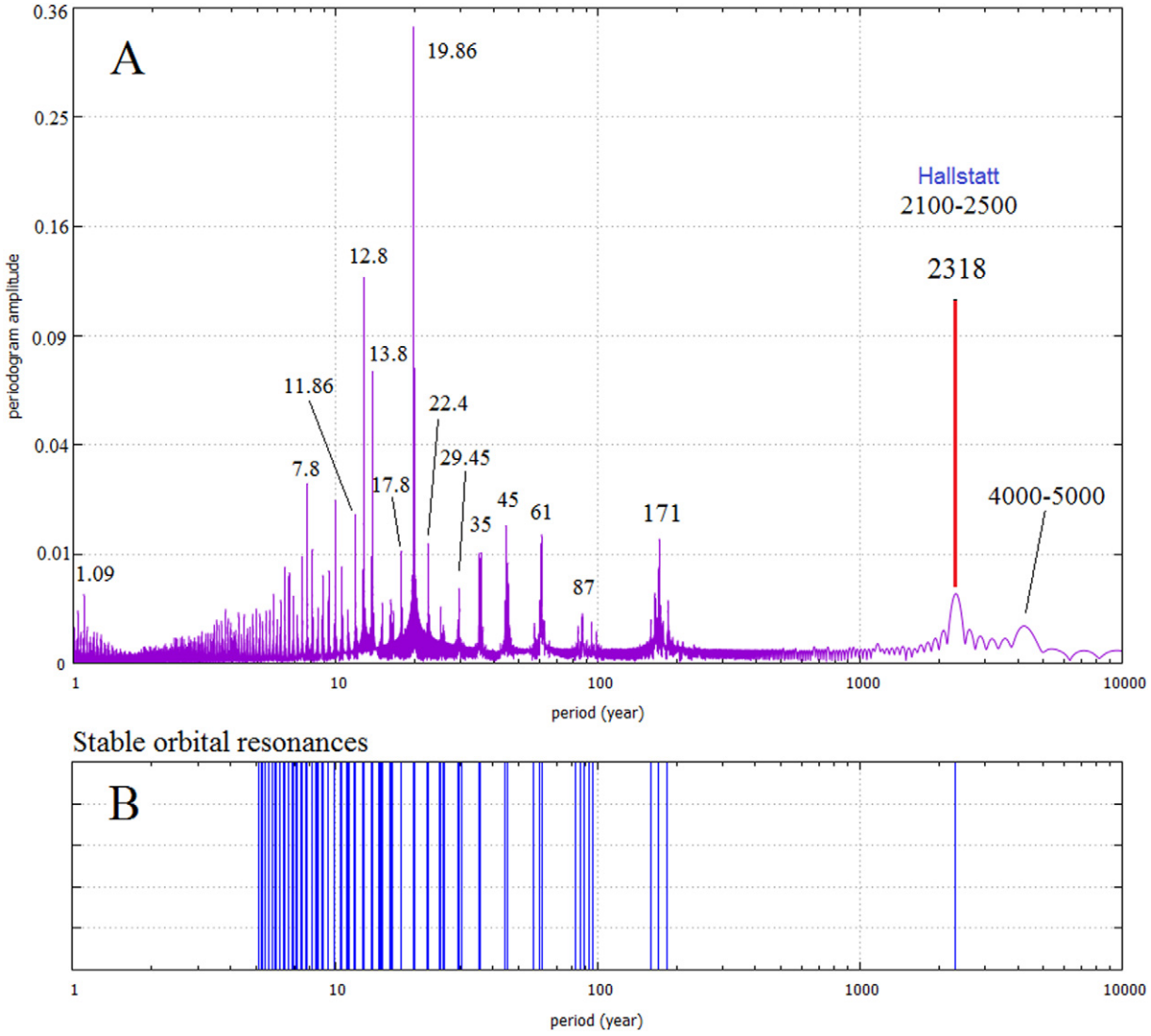

Fig. 4. [A] Periodogram of the eccentricity record of the Sun-PMC orbit depicted in Fig. 3. The spectral peak corresponding at the Hallstatt period at 2318 years is well visible. Also a quasi 20-year oscillation, a quasi 60-year oscillation, the 82-97 year Gleissberg oscillation and the 159-185 year Jose oscillation (and others) are observed well. [B] The blue bars represent the period of stable planetary resonances of the solar system generated by Jupiter, Saturn, Uranus and Neptune for period larger than 5: see also Table 1. Note the accurate correspondence between these resonances and the spectral peaks depicted in [A]. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

statistically more circular (lower list of lower panels, the average eccentricity is $e \approx 0.590$). The chosen time intervals were 344 years long that is twice the 172 year harmonic revealed in the periodogram of Fig. 4. The upper list of these panels reveals that during these periods the Sun-PMC orbits are skewed with large regions that are rarely visited and the trajectory appears developing mostly within a 5 AU radius, which is the orbit of Jupiter, but sometimes it also clearly exceeds the 7 AU radius distance from the Sun (red curve). The lower list of panels reveals that during these periods the Sun-PMC orbits are more regular, more circular, symmetric and more uniformly cover all areas within a 7 AU radius distance from the Sun.

The dynamics observed in Fig. 5 is also reminiscent at the larger Hallstatt time scale of the trefoil ordered and disordered state of the inertial motion of the Sun which is correlated to the grand maxima and minima of solar activity, respectively, as suggested by Charvátová (2000, 2009) inspired by the 178.7 year cycle found by Jose (1965). However, as Fig. 5 shows, here it is during the transition periods from an orbital state to the other that correlates with periods of maximun or minimum radionucleotide production.

7. Analysis of the pericycle and apocycle orbital arcs

The solar system pulses driven by the revolution of its planets around the Sun and the major harmonic period of this dynamics within the 200–10,000 year time scale is 2318 years. This period perfectly corresponds to the 2100–2500 year Hallstatt oscillation. However, in the chosen observable - the eccentricity variation of the Sun-PMC orbits - this slow oscillation is relatively small: to make it visible in Fig. 3 we needed to plot it magnified by 10.

It is important to search for a more specific astronomical origin for the Hallstatt-cycle that could stress the above dynamical characteristics of the Sun-PMC orbit. The search for a more appropriate orbital proxy is addressed in this section.

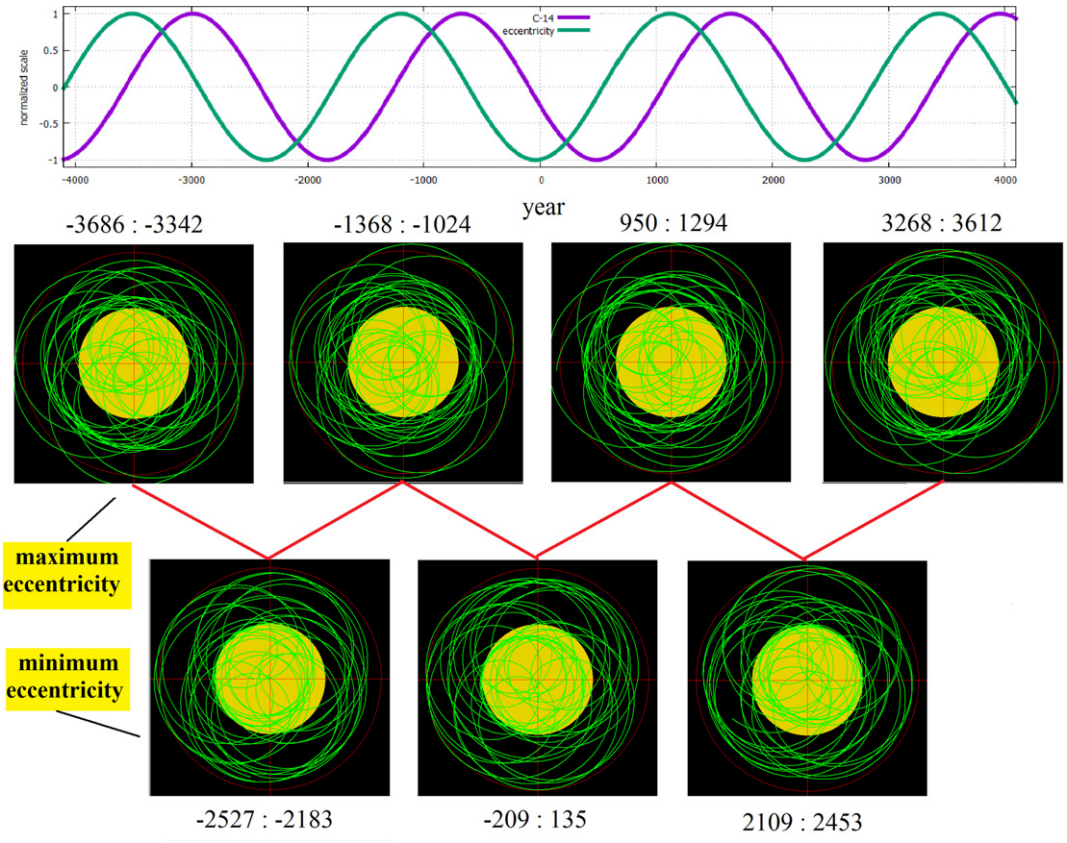

Fig. 5. (Top) 2300–2400 year harmonics referring to the $\Delta^{14}C$ (‰) record depicted in Fig. 1 and the eccentricity record depicted in Fig. 3. Note the $\pi/2$ phase shift. (Bottom) Trajectory of the PMC relative to the Sun during intervals of 344 years referring to periods of the eccentricity maxima (above, more disordered, open orbits) and minima (below, more ordered, closed orbits). The yellow disk radius is about 3.5 AU, while the red circle radius is about 7 AU. The transition periods (red segments) from the eccentricity maxima to minima correspond to maxima in radionucleotide production, while the transition periods from the eccentricity minima to maxima correspond to minima in radionucleotide production. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

As evident in Fig. 6, the Sun-PMC dynamics is characterized by a series of unit cycles made of an apocycle, or external large orbit, and a pericycle, or internal small orbit (cf. Piovan and Milani, 2006). During each apocycle the PMC moves in an arc in which it reaches a maximum speed and distance from the Sun. In the following pericycle the PMC enters into a helical coil in which it reaches a minimum speed and distance from the Sun before returning to a position very near to the point where it has entered in the pericycle. This exit point is the beginning of the following apocycle. Fig. 6 shows 4 consecutive full (apocycle plus pericycle) orbits from 10/6/1976 to 17/11/2055.

The orbit sections depicted in Fig. 6 vary substantially in time. Sometimes the apocycles are very different from the pericycle (as in the figure). Other times they have similar amplitudes. This variation is due to the relative position of the various planets, in particular of the large Jovian ones. Let us investigate in details the dynamics of these apocycles and pericycles.

Fig. 7A shows the time periods of the subsequent apocycles, P_a, while Fig. 7B shows those of the following pericycles, P_p. The apocycle periods average about $\mu_a = 9.91$ years and vary from this mean up to a ± 1.5 years while the pericycle periods average about $\mu_p = 9.95$ years and vary from their mean up to a ± 0.5 years. The sum of the two average periods is 19.86 years that corresponds to the conjunction period between Jupiter and Saturn. The upper panel of Fig. 7 shows an Hallstatt oscillation at 2318 year period found in $\Delta^{14}C$ (‰) record, as depicted in Fig. 1B, to show that its phase is about $\phi = \pi/2$ and $\phi = -\pi/2$ with the beat oscillation depicted in the lower A and B panels, respectively.

Fig. 8A and B depicts two records calculated from the periods depicted in Fig. 7A and B, respectively, as the square of the volatility from their mean μ, that is as: $(\Delta P_a)^2 = (P_a - \mu_a)^2$ and $(\Delta P_p)^2 = (P_p - \mu_p)^2$, respectively. This operation was chosen to make even more evident the 2100–2500 year oscillation present in these records. The upper panel of Fig. 8 shows the Hallstatt oscillation found in $\Delta^{14}C$ (‰) record, as depicted in Fig. 1B, to show that its phase is about $\phi = \pi/2$ and $\phi = -\pi/2$ with the oscillation depicted in the lower A and B panels, respectively.

Finally, Fig. 9A shows, for each full apocycle plus pericycle unit, the times requested by the PMC to move from the minimum to the following maximum distance from the Sun. Fig. 9B, instead, shows for each orbit the times requested by the PMC to move from the maximum to the following minimum distance from the Sun. The upper panel of Fig. 9 depicts the Hallstatt oscillation found in $\Delta^{14}C$ (‰) record, as in Fig. 1B, to show that its phase is about $\phi = 0$ and $\phi = \pi$ with the oscillation depicted in the lower A and B panels, respectively.

The time sequences depicted in Figs. 7–9 clearly put in evidence a strong oscillation of about 2318 years. Fig. 7 reveals the presence of a major beat frequency with such a period, while Figs. 8 and 9 reveal a direct 2318 year oscillation. Moreover, the phase coincidence observed in Fig. 9 between the Hallstatt oscillation found in $\Delta^{14}C$ (‰) record and in that observed in the astronomical record suggests that on the 2100–2500 year time scale the cosmic ray flux reaching the Earth is higher, when during intervals of about 172 years, within the pericycle-apocycle orbits, the time required by

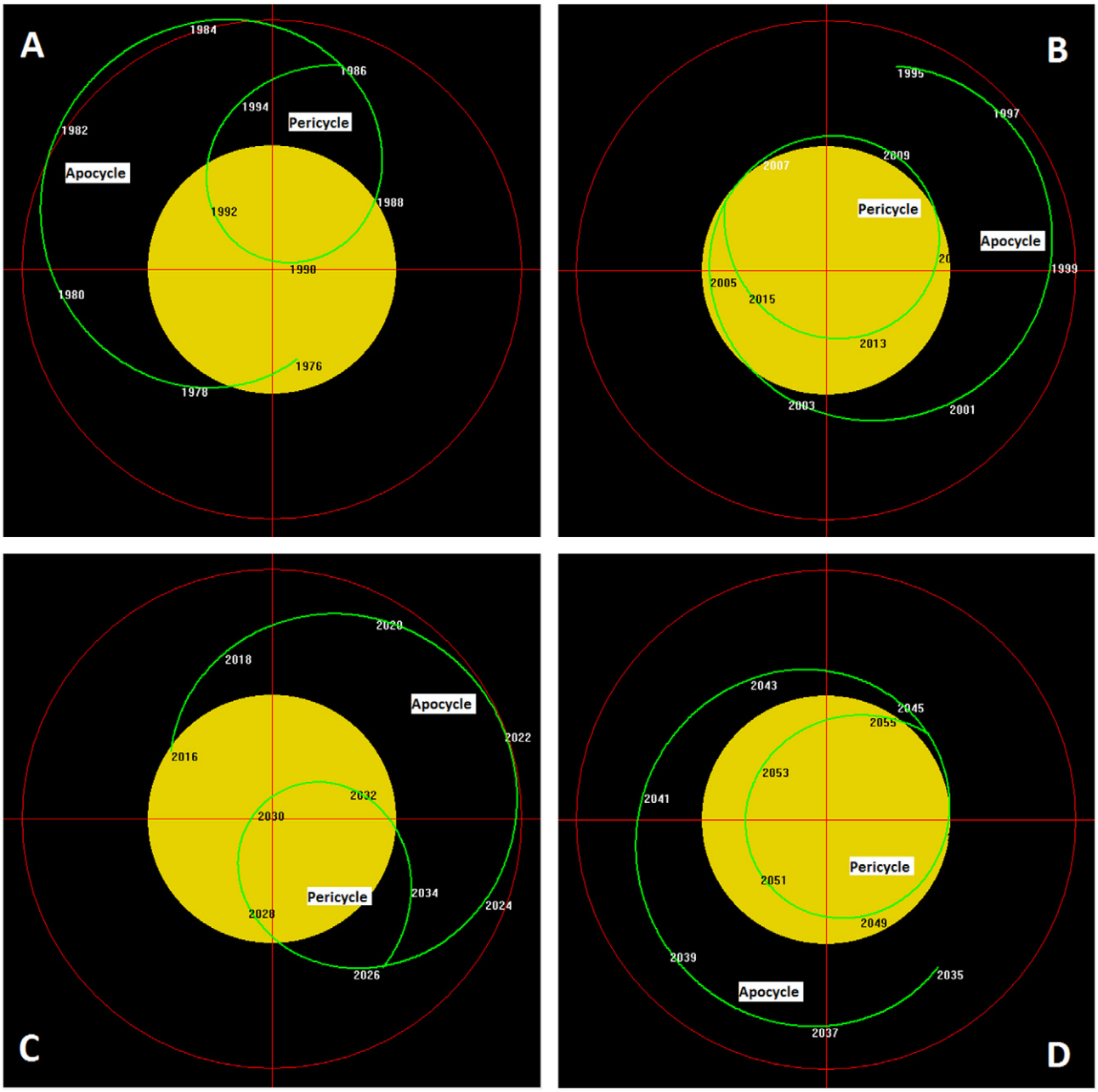

Fig. 6. Motion of the PMC relative to the Sun from 10/6/1976 to 17/11/2055. The diagrams depict four contiguous orbits made of one apocycle (external larger orbit) and one pericycle (internal smaller orbit). (Solar Orbit Simulator, http://arnholm.org/astro/sun/sc24/sim1/). The yellow disk radius is about 3.5 AU, while the red circle radius is about 7 AU. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

the PMC to move from the minimum to the maximum distance from the Sun varies from about 8 to 16 years while the time required by the PMC to move from the maximum to the minimum distance from the Sun varies from about 7 to 14 years; on the contrary, the minima of the radionucleotide production occurred, when the time required by the PMC to move from the minimum to the maximum distance from the Sun varies from about 7 to 14 years while the time required by the PMC to move from the maximum to the minimum distance from the Sun varies from about 8 to 16 years.

The power spectra functions depicted in Fig. 10 show that the $\Delta^{14}C$ record depicted in Fig. 1B and the Sun-PMC orbital records depicted in Figs. 7–9 share a very large common frequency peak at 2100–2500 year period centered at the stable orbital resonance of 2318 years. These spectral peaks have a 95% statistical confidence against red-noise background (Ghil et al., 2002).

Fig. 10 shows also that the radionucleotide record presents a significant 900–1050 year Eddy oscillation that has been extensively found in ^{14}C, ^{10}Be and climate records throughout the Holocene (Bond et al., 2001; Kerr, 2001) and has been modeled involving the orbits of Jupiter and Saturn and the 11-year solar cycle (Scafetta, 2012a, 2014). The additional multi-secular minor spectral peaks present in the $\Delta^{14}C$ record are not further discussed here, but they have been also found among the planetary harmonics such as the following periods: 104, 130, 150, 171, 185, 208, 354, 500–580 years (e.g.: Abreu et al., 2012; Scafetta, 2014). Fig. 10 also reveals that the chosen orbital measures present spectral peaks at about 159 years

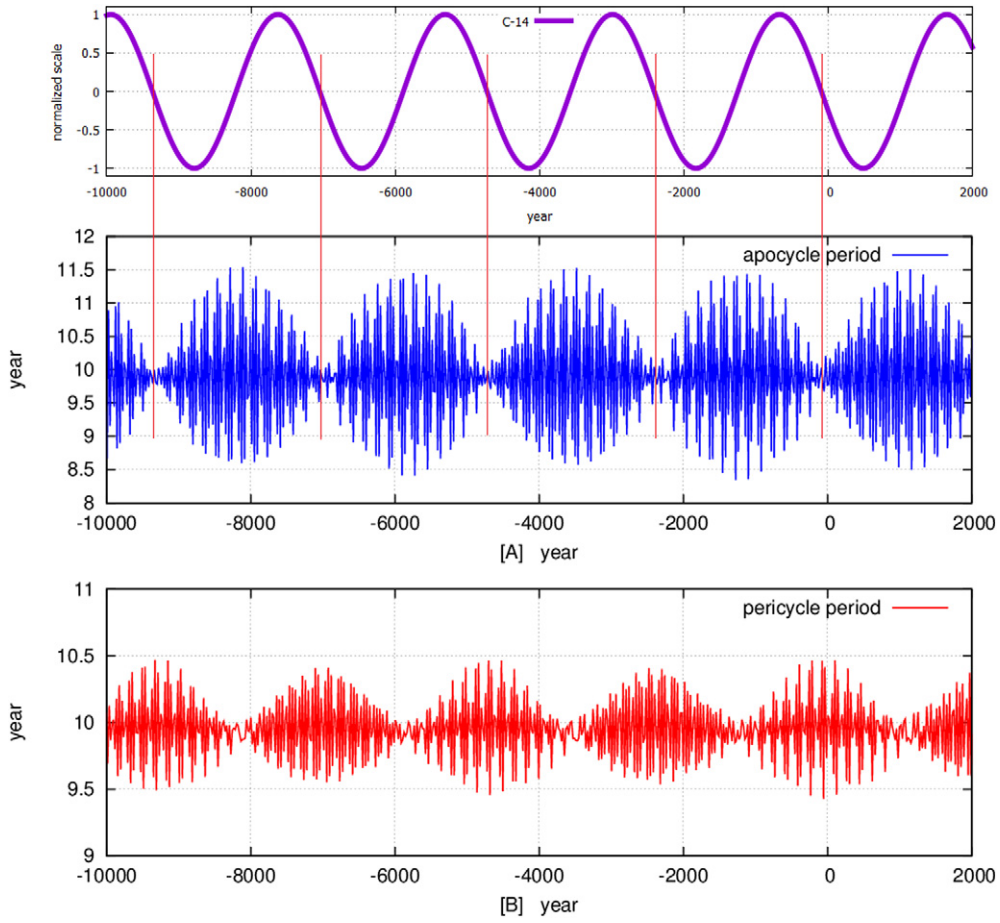

Fig. 7. Upper panel: the Hallstatt oscillation found in $\Delta^{14}C$ (‰) record, as depicted in Fig. 1B. Lower panels show the time periods of the apocycles [A] and pericycles [B] of the PMC relative to the Sun. The upper panel Hallstatt oscillation is approximately in phase quadrature ($\phi = \pi/2$ and $\phi = -\pi/2$) with the beat oscillation depicted in the lower panels as the red vertical lines show. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

(from Fig. 7A), 171–172 years (from Fig. 8A) and 185 years (from Fig. 9A), which are also stable orbital resonances as discussed in Section 3. The 171–172 and 185 year periods are visible in the $\Delta^{14}C$ record although very small, but they appear well in other solar records (cf.: McCracken et al., 2014; Sharp, 2013).

Fig. 11 shows the continuous wavelet transforms of the records depicted in Figs. 1B, 7A, 8A and 9A, respectively. Also these four panels show that the four records share a significant harmonic at about 2100–2500 year period.

Finally, we study the spectral coherence between the $\Delta^{14}C$ record and the chosen astronomical records. Fig. 12 shows in the left panels the cross wavelet transform (XWT) and in the right panels the wavelet coherence (WTC) between the $\Delta^{14}C$ record depicted in Fig. 1B and each of the Sun-PMC motion records depicted in Figs. 7A, 8A and 9A, respectively (Grinsted et al., 1566). The cross wavelet transform finds regions in time frequency space where the time series show high common power. The wavelet coherence finds regions in time frequency space where the two time series co-vary but does not necessarily have high power.

As clearly shown in Fig. 12, the six panels demonstrate that the $\Delta^{14}C$ record and the chosen astronomical records share a coherent frequency at about 2100–2500 year period with a 95% statistical confidence against red noise background.

8. Discussion and conclusion

Several experimental evidences demonstrate that throughout the Holocene the ^{14}C atmospheric concentration has varied cyclically in time (e.g. Damon and Linick, 1986; Houtermans, 1971; Kromer et al., 1998, and many others). An observed large oscillation has a period of about 2100–2500 years. This oscillation is known in the scientific literature as the Hallstatt cycle. As discussed in the Introduction, the presence of a fundamental harmonic at such a period has been confirmed in numerous studies and found also in ^{10}Be and climate records. For example, recently McCracken et al. (2013) confirmed an oscillation with period centered between 2300 and 2320 using Fourier amplitude spectrum for GRIP ^{10}Be, the modeled estimate of the ^{14}C production rate and the modulation function (in MeV) computed from the EDML and GRIP ^{10}Be data, and the INTCAL09 ^{14}C record.

A fundamental scientific issue is to understand the origin of such an oscillation. It is legitimate to claim that it is an internal climate or solar oscillation, but in the absence of an explicit physical mechanism this interpretation remains an unproven hypothesis. This leaves open the possibility for an external astronomical origin of the observed oscillation. It is observed that the only well-known harmonic generator of the solar system is provided by the gravitational and electromagnetic oscillations induced by the revolution of the planets around the Sun.

Thus, we have hypothesized that the Hallstatt oscillation found in radionucleotide and climatic records could be the result of a specific orbital resonance within the solar system. A search of the stable resonances involving the four outer giant planets - Jupiter, Saturn, Uranus and Neptune - has determined that, indeed, there exists a major stable resonance with a period of 2318 years. This stable resonance is also the only one for period larger than 200 years among those

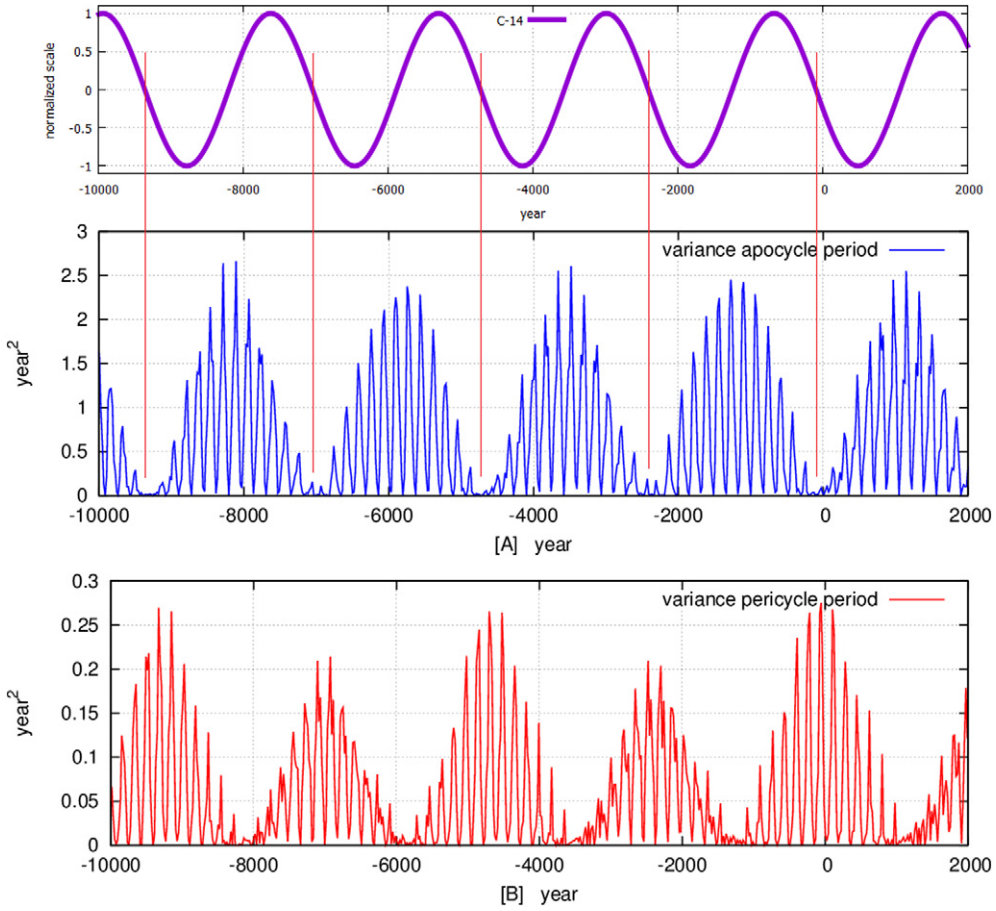

Fig. 8. Upper panel: the Hallstatt oscillation found in $\Delta^{14}C$ (‰) record, as depicted in Fig. 1B. Lower panels: [A] and [B] are calculated from the records depicted in Fig. 7A and B, respectively, as the square of their volatility from the mean. The upper panel Hallstatt oscillation is approximately in phase quadrature ($\phi = \pi/2$ and $\phi = -\pi/2$) with the oscillation depicted in the lower panels as the red vertical lines show. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

listed in Table 1. Since this resonance is perfectly coherent to the Hallstatt oscillation found in radionucleotide and climate records, this is unlikely a coincidence: we can name this resonance as the Hallstatt H-resonance of the solar system.

We have also theoretically determined a large number of additional stable orbital resonances of the solar system and many of their periods (e.g. about 20 years, 44–46 years, 57–62 years, 82–97 years, 159–171–185 years) are also typically found in solar, aurora and climate records throughout the Holocene (e.g.: McCracken et al., 2014; Ogurtsov et al., 2002; Scafetta, 2014; Scafetta and Willson, 2013a; Sharp, 2013; Vaquero et al., 2002, and many others).

Inspired by the Milanković's (1930) theory linking the variation of the Earth's orbit eccentricity to the glacial cycles, we tested whether the Hallstatt cycle could derive from, and therefore be revealed by, the overall variation of the circularity of the solar system that could eventually modulate the solar wind intensity and direction and therefore also the incoming cosmic ray flux and the interplanetary dust concentration around the Earth. We chose to study the orbit of the planetary mass center (PMC) relative to the Sun and used the instantaneous eccentricity vector function (e.g. Mungan, 2005) applied to the Sun-PMC orbit to determine the eccentricity variation of this virtual planet from 13,000 BCE to 17,000 CE. Using spectral analysis we have demonstrated that this observable presents a significant oscillation with a 2318 year period together with a number of already known oscillations associated to the orbital periods of the planets at scale shorter than 200 years. Fig. 4 stresses that the 2318 year period peak is the most relevant in the spectral range between 200 and 10,000 years indicating that this oscillation dominates this time scale range. Thus, there exists a rhythmic contraction and expansion pattern of the solar system induced by the planets; this pulse is spectrally coherent to the Hallstatt oscillation found in nucleotides and climate records.

In particular, we found a $\pi/2$ phase shift between the 2100–2500 year curves present in the variation of ^{14}C record and the solar system eccentricity function. Thus, on the Hallstatt-cycle time scale a larger production of radionucleotide particles, i.e. the occurrence of a stronger cosmic rays flux toward the inner region of the solar system, occurs while the Sun-PMC orbit evolves from statistically more elliptical shapes ($e \approx 0.598$) to statistically more circular ones ($e \approx 0.590$). Thus, while the system is slowly imploding or bursting inward. Analogously, a smaller production of radionucleotide particles, i.e. the occurrence of a weaker cosmic ray flux toward the inner region of the solar system, occurs while the Sun-PMC orbit evolves from statistically more circular shapes ($e \approx 0.590$) to statistically more elliptical ones ($e \approx 0.598$). Thus, while the system is slowly exploding or bursting outward.

Finally, to better identify an astronomical proxy able to greatly stress the 2318-year H-resonance, we analyzed how the pericycles and apocycles of the Sun-PMC orbits evolve (Piovan and Milani, 2006). We found that the time series of the periods of these orbits are characterized by a very prominent 2318 year oscillation that is perfectly coherent with the Hallstatt oscillation found in the investigated $\Delta^{14}C$ record with a statistical confidence above 95%. These orbital proxies are also characterized by prominent 159, 171–172,

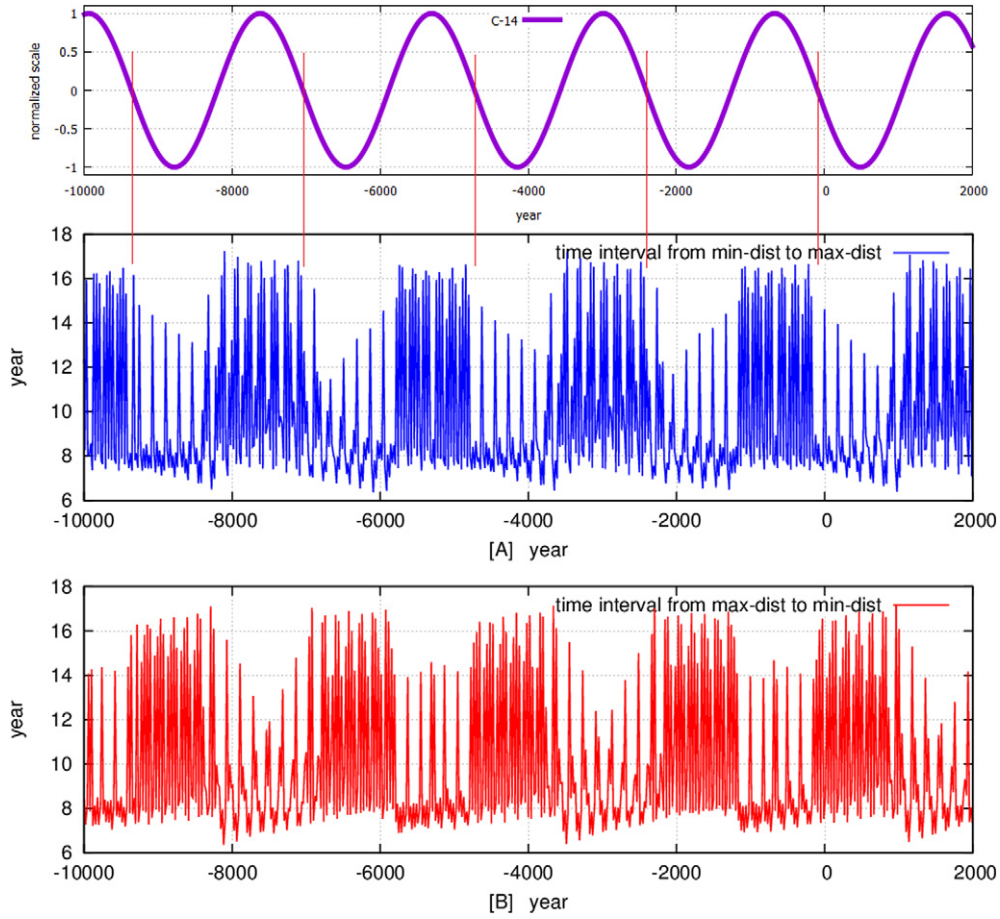

Fig. 9. Upper panel: the Hallstatt oscillation found in $\Delta^{14}C$ (‰) record, as depicted in Fig. 1B. Lower panels: [A] Sequence of time intervals requested by the PMC to move from its minimum to its maximum distance from the Sun; [B] sequence of time intervals requested by the PMC to move from its maximum to its minimum distance from the Sun. The upper panel Hallstatt oscillation is approximately in phase ($\phi = 0$ and $\phi = -\pi$) with the oscillation depicted in the lower panels as the red vertical lines show. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

and 185 year oscillations, which correspond to other stable resonances of the solar system. Major harmonics within this spectral range, which was first identified by Jose (1965), is found in long solar activity proxy records (Solanki et al., 2004; Steinhilber et al., 2009) and in long historical aurora records (Scafetta and Willson, 2013a). The coherence at this time scale between our model and the data is revealed in Fig. 12 by the WXT methodology. Other periodicities found in the eccentricity vector function of the Sun-PMC orbit, such as about the 20, 30, 45, 60, 87 year periods, are typically found among solar (cf. Ogurtsov et al., 2002), aurora and climate indexes (cf.: Scafetta, 2010, 2012c, 2013; Scafetta and Willson, 2013a).

We found (e.g. Fig. 9) that at the Hallstatt cycle maxima of the radionucleotide production occurred when the time required by the PMC to move from the minimum to the maximum distance from the Sun varies from about 8 to 16 years, while the time required to move from the maximum to the minimum distance varies from about 7 to 14 years throughout the full pericycle-apocycle pattern. On the contrary, the minima of the radionucleotide production occurred when the time required by the PMC to move from the minimum to maximum distance from the Sun varies from about 7 to 14 years while the time required by the PMC to move from the maximum to the minimum distance from the Sun varies from about 8 to 16 years. This suggests that, at this time scale, the cosmic ray flux increases (decreases) during periods of slower (faster) expansion and faster (slower) contraction of the Sun-PMC orbit wobbling. Thus, a faster expansion of the solar system prevents cosmic rays to enter in its inner regions, while a faster contraction favors a larger incoming of cosmic rays. This suggests a rhythmic modulation of the geometry of the heliopause and/or of solar wind termination shock and, therefore, of the heliospheric magnetic field (Owens and Forsyth, 2013), which in the former case should become larger while in the latter should become smaller, inducing a larger or smaller deviation of the incoming cosmic rays, respectively.

Fig. 13 shows a graphical representation of the heliosphere of the solar system with highlighted the solar wind termination shock, the heliopause, the bow shock and the incoming interstellar wind. A reader should note that the heliosphere is not stationary relative to the incoming cosmic rays, but it is wobbling like the Sun-PMC orbits that we have studied in this work. Since the planetary system is within the heliosphere this means that the interaction of the planets with the inner heliosphere can be relevant. In particular, magnetic field reconnections can capture and redirect solar wind shaping the heliosphere, which modulates the cosmic ray flux. The imploding-exploding dynamics revealed in our record could easily modulate the solar wind termination shock surface and, therefore, modulate the incoming cosmic ray flux. Potgieter (2013) summarizes mechanisms of solar modulation of cosmic rays in the heliosphere.

There is a related but complementary mechanism. The displacements of the planets could directly or indirectly modulate the amount of interplanetary/cosmic dust falling on Earth. The cosmic-planetary dust is concentrated within the disk of the solar system where the Sun-PMC orbit evolves, including the region surrounding the Earth-Moon system, and regulates the intensity of the zodiacal light (cf.: Ermakov et al., 2009a,b; Ollila, 2015). In fact, every day

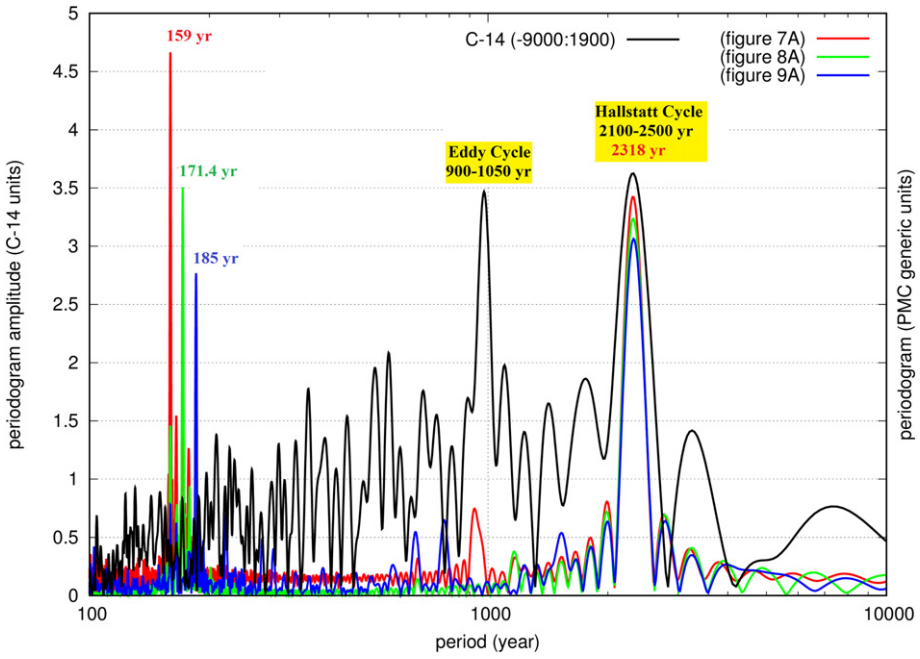

Fig. 10. (Black curve) Periodogram of the $\Delta^{14}C$ record from −9000 BCE to 1900 CE that is depicted in Fig. 1B. (Colored curves) Same for the Sun-PMC orbital records depicted in Figs. 7A, 8A and 9A spanning from 10,000 BCE to 10,000 CE. Note the common spectral peaks at 2100–2500 year period which are centered at the orbital resonance period of 2318 years. The three peaks on the left are at about 159 years, 171.4 years and 185 years: the orbital resonances discussed in Section 3. The Eddy and Hallstatt spectral peaks have a 95% statistical confidence with respect to a red-noise background using the Multi Taper Method, MTM (Ghil et al., 2002). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

from 400 to 10,000 tons of dust enters in the Earth's atmosphere. The sizes of these particles vary from 0.001 μ m to several hundreds of micrometers and they are mostly made of common elements such as Fe, Mg, S, Al, Ca, and Na. Because these particles are very likely also charged by solar wind, they should be subject not only to gravitational forces but also to magnetic fields and to the solar wind itself (Divari, 1966). Therefore, interplanetary/cosmic dust can be driven by the planets (Divari, 1966). Once that these charged particles enter the Earth's atmosphere, they behave as efficient condensation nuclei of the atmospheric water vapor, which is a polarized molecule, in particular Mg, S, and Na, and also help in forming clouds (cf.: Ermakov et al., 2009a,b; Ollila, 2015). The Sun-PMC wobbling could more easily disperse this dust away from the inner region of the solar system when its orbit expands fast and contracts slower as depicted in Fig. 9 inducing the formation of less clouds on the Earth, and vice versa. Indeed, while long records of interplanetary/cosmic dust falling on Earth are not available to test this hypothesis, a record of historically recorded meteorite falls in China from 619 to 1943 CE has revealed harmonics such as 10.5, 14–15, 30 and 60–63 year oscillations (Scafetta, 2012c; Yu et al., 1983), which are also found among the main harmonics of the eccentricity function of the Sun-PMC orbit and among the stable resonances of the solar system (see Table 1). A modulation of the interplanetary/cosmic dust density surrounding the Earth-Moon system driven by the solar wind and the planets' magnetospheres may also contribute to explain why the Hallstatt cycle, and a number of other oscillations revealed in Fig. 4, are also observed in climate records (e.g.: Levina and Orlova, 1993; OBrien et al., 1995). Further research will better clarify the specific physical mechanisms involved in these processes.

In conclusion, our results clearly suggest that the velocity of the displacements of the Jovian planets (Jupiter, Saturn, Uranus and Neptune), which mainly determine the inertial motion of the Sun on the long time scales, also influences the solar activity and the intensity of its solar wind, and/or modifies the structure of the heliosphere. The latter would then modulate the incoming cosmic ray flux that produces radiocarbon and/or interplanetary/cosmic dust concentration and, simultaneously, they would regulate the Earth's climate by modulating the cloud system: see the schematic flow chart depicted in Fig. 14. This synchronization phenomenon is likely favored by the fact that the observed oscillations are stable orbital resonances of the solar system. A possible chain of the involved mechanisms has been suggested by some authors (Kirby, 2007; Ollila, 2015; Scafetta, 2012c, 2013; Shaviv et al., 2014; Svensmark, 1998; Svensmark et al., 2009; Tinsley, 2008). The fact that a specific set of planetary resonances may be modulating heliospheric, solar and climatic records may also suggest why these records appear linked at multiple time scales, and even at the short ones (e.g.: Scafetta et al., 2004; Scafetta and West, 2006; Scafetta, 2009).

Although it is still uncertain how the planets could influence solar activity, the cosmic ray flux and/or the dust reaching the Earth, a planetary origin of solar and climate oscillations, which has been proposed since antiquity, has recently received a renewed attention in the scientific literature. Planetary theories of climate variations were widespread in ancient times and, in more recent times, a planetary theory of solar variation was proposed by Wolf (1859) to explain the 11-year solar cycle. Wolf hypothesized that the just discovered 11-year solar cycle could emerge from a combined influence of Venus, Earth, Jupiter and Saturn, which has been recently confirmed (Hung, 2007; Scafetta, 2012a,b; Wilson, 2013). Stefani et al. (2016) speculated that the tidal oscillation of 11.07 years induced by the Venus–Earth–Jupiter system may lead to a 1:1 resonant excitation of the oscillation of the α-effect. In general, a planetary origin of solar and climate oscillations is based on numerous empirical evidences at multiple time scales and some preliminary physical explanations (e.g.: Abreu et al., 2012; Charvátová, 2009; Cionco and Soon, 2015; Hung, 2007; Jakubcová and Pick, 1986; Jose, 1965; McCracken et al., 2013, 2014; Mörner, 2013, 2015; Puetz et al., 2014; Salvador, 2013; Scafetta, 2010, 2012a,b, 2013, 2014, 2016; Scafetta and Willson, 2013a,b; Sharp, 2013; Solheim, 2013; Tan and Cheng, 2013; Tattersall, 2013a; Wilson, 2013).

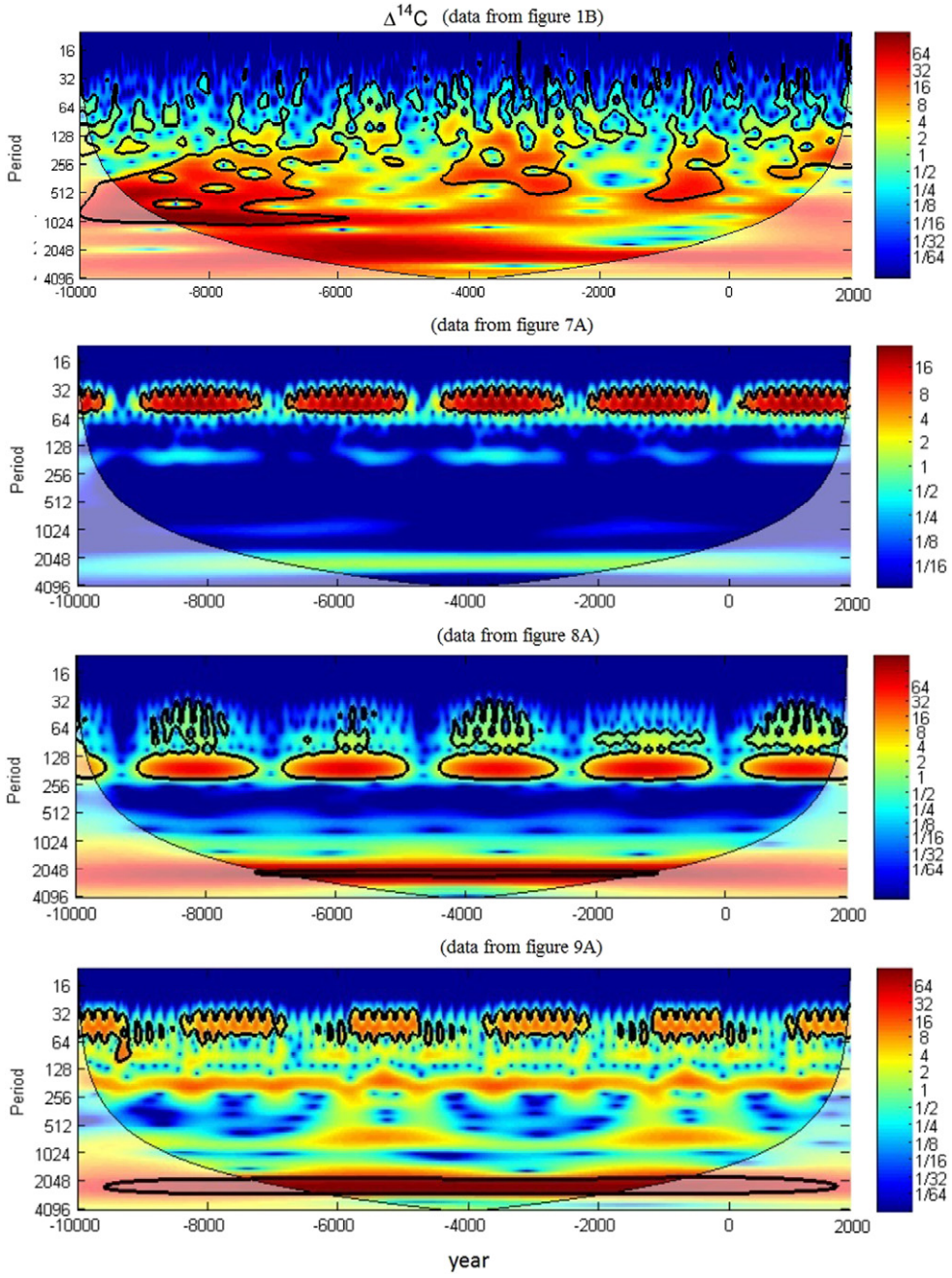

Fig. 11. Continuous wavelet transforms of the records depicted in Fig. 1B, 7A, 8A and 9A, respectively.

Since the 19th century, the planetary theory of solar and climate variations has also received a number of critiques (some of the most recent critical studies include: Cameron and Schüssler, 2013; Cauquoin et al., 2014; Callebaut et al., 2012; Holm, 2014, 2015; Poluianov and Usoskin, 2014; Smythe and Eddy, 1977). However, several rebuttals of the critiques have also been published. The rebuttals can be summarized as follows: i) the Sun can react to a planetary tidal forcing because it is a nuclear fusion generator that might greatly amplify the modest gravitational tidal effect (e.g.: Scafetta, 2012b; Wolff and Patrone, 2010); ii) an additional electromagnetic coupling could link the Sun to the planets throughout the solar wind (e.g.: Scafetta and Willson, 2013b); iii) the solar-climate physics occurs throughout some heliospheric dynamics (e.g.: Scafetta and Willson, 2013a,b); iv) the coupling between some astronomical and the solar-climate harmonics is very good when the appropriate astronomical proxies that take into account multiple planets are constructed (e.g.: Scafetta, 2014, 2016; Sharp, 2013; Wilson, 2013); v) the spectral coherence at the given harmonics is statistically significant above 95% when the calculations are done correctly and once the limits of the used analysis algorithms are properly considered (see also: Scafetta, 2014, 2016); Monte Carlo techniques used to test the likelihood that multiple frequencies in solar records match planetary records show unambiguously that this probability is lower than 10^{-4} (e.g.: Abreu et al., 2014; Scafetta and Willson, 2013b).

We also noted that once challenged, some critical authors responded by contradicting their previous claims. For example, Callebaut et al. (2012) argued against a planetary origin of the solar oscillation by also claiming that the five major identified solar periodicities - Schwabe (~11 years), Hale (~22 years),

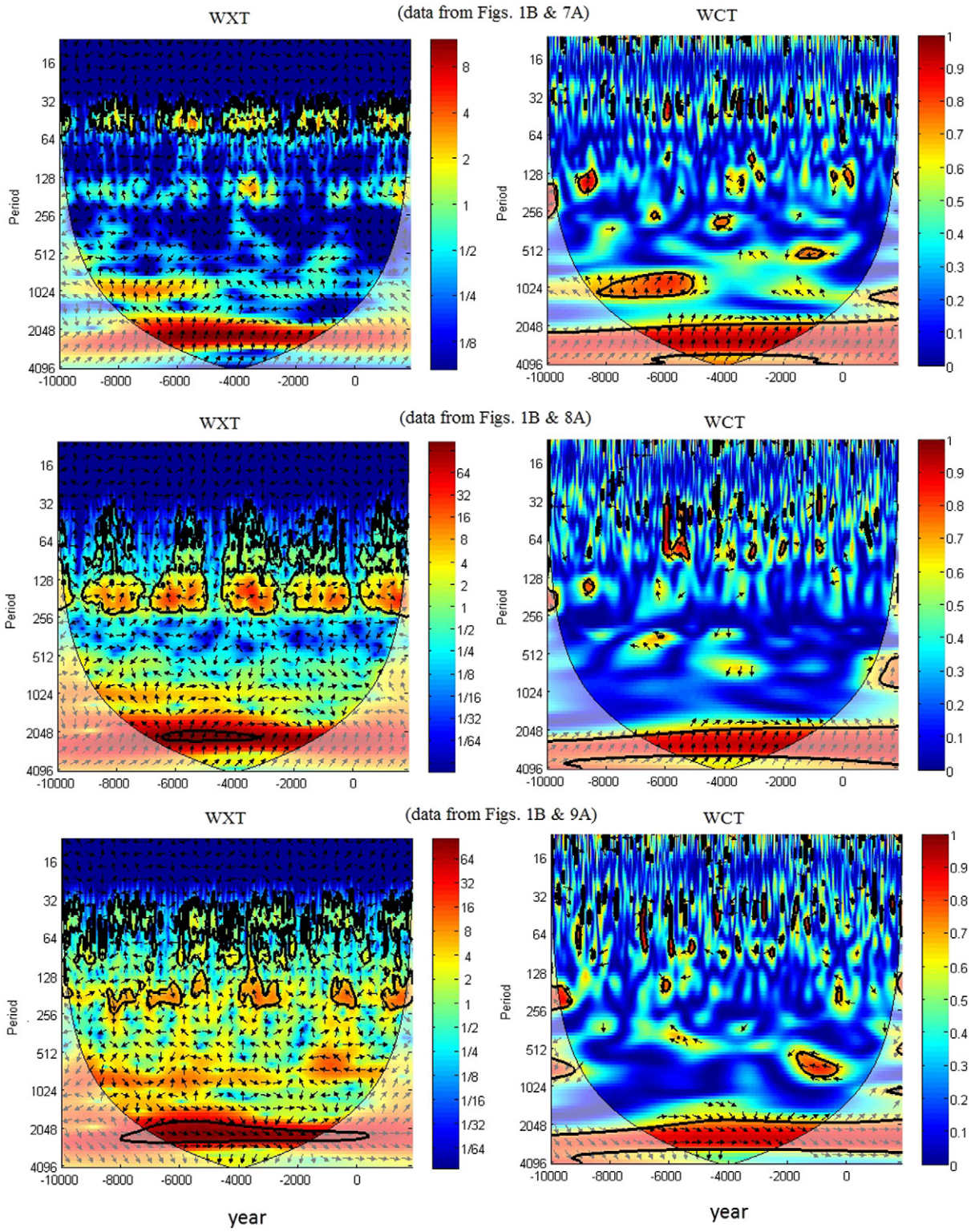

Fig. 12. (Left panels) The cross wavelet transform (XWT) and (right panels) the wavelet coherence (WTC) between the $\Delta^{14}C$ record depicted in Fig. 1B and each of the Sun-PMC motion records depicted in Figs. 7A, 8A and 9A, respectively. The red areas surrounded by the black line satisfy the 95% confidence level. (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)

Gleissberg (~88 years), Suess (~203–208 years) and Hallstatt (~2300–2400 years) cycles - were never successfully reproduced by papers advocating planetary influences on solar variability. However, when their claim was challenged (e.g.: Scafetta et al., 2013), Callebaut et al. (2013) acknowledged that *"it is well-known that there are some periodicities that are common to solar activity and planetary motions"* which make his further critique very weak as explained in Scafetta et al. (2013). The present work also contradicts Callebaut et al. (2012). Similarly, Holm (2014) argued that using windowed periodograms no spectral coherence between temperature

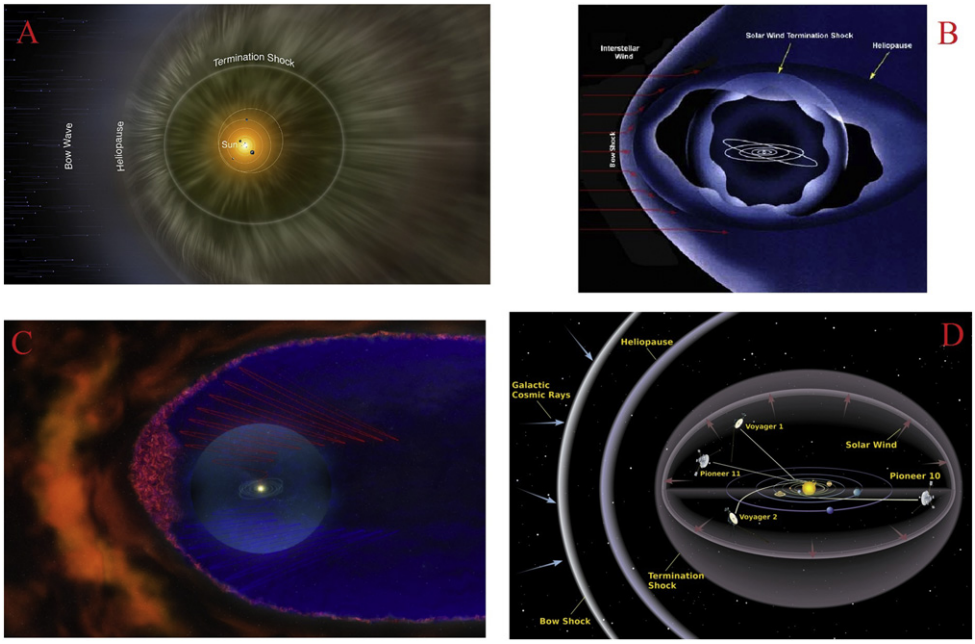

Fig. 13. Artist representations of the heliosphere of the solar system with highlighted the solar wind termination shock, the heliopause, the bow shock and the incoming interstellar wind, that is the cosmic ray flux which is mostly deflected at the heliopause. These surfaces wobble together with the Sun and the planets. These illustrations shows how the sun's activity pushes out cosmic radiation from outside of the solar system. These and other artist representations of the heliosphere have been published by NASA (credit to Howell, 2014; Phillips, 2011, and others).

records and the speed of the solar center of mass could be found at given frequencies such as at 20 year and 60 year periods. However, after that Scafetta (2014) demonstrated that Holm used improperly the windowed periodogram, that is, he used it with too short window segments to detect the signals, Holm (2015) acknowledged that *"it is not hard to produce high coherence estimates at periods around 15–22 and 50–60 years between these data sets."* Rebuttals of Holm's (2015) further critiques were presented in Scafetta (2016).

Although several issues remain open to further investigations, the published scientific literature provides several evidences that solar and climate records are characterized by periodicities that are common to planetary motions at multiple time scales from a few months to several millennia. Moreover, no alternative explanations of these oscillations have been proposed by the critics. In other words, an alternative theory explaining the observed oscillations simply does not exist. The methodologies and results of the present paper contribute to this discussion showing compelling evidences that also the long Hallstatt (2100–2500 years) oscillation likely has an astronomical origin linked to the internal dynamics of the solar system and its stable resonances including those produced

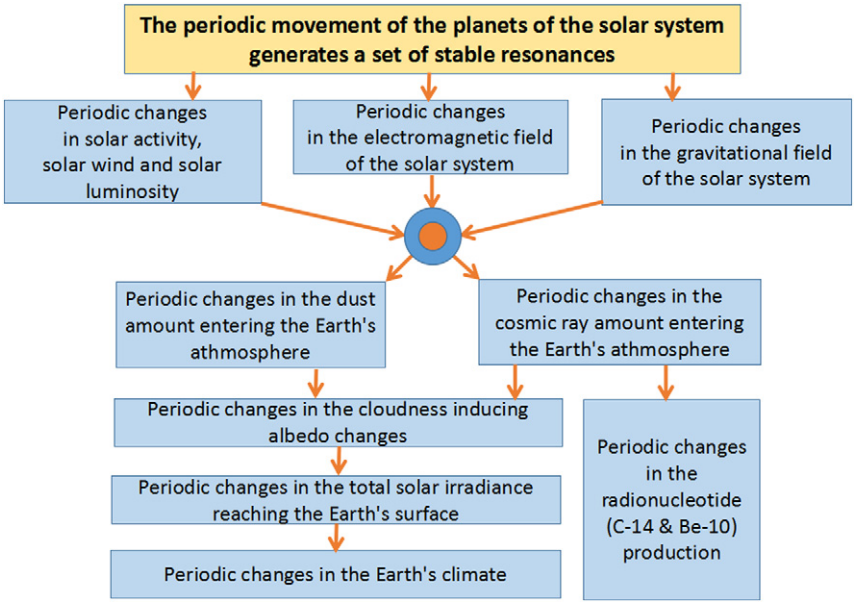

Fig. 14. Schematic flow chart explaining a chain of mechanisms linking the periodic movement of the planets around the Sun with periodic changes in solar activity and climate change.

by Jupiter, Saturn, Uranus and Neptune at periods of 159 years, 171 years, 185 years and 2318 years. From Fig. 5, the next Hallstatt minimum in the ^{14}C cosmogenic radioisotopes will occur around 2804 CE and the next maximum around 3963 CE.

Acknowledgments

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